

Low-Level Copy Number Analysis

CRMA v2 preprocessing

Henrik Bengtsson

Post doc, Department of Statistics,
University of California, Berkeley, USA

CEIT Workshop on SNP arrays,
Dec 15-17, 2008, San Sebastian

Copy-number probes are used to quantify the amount of DNA at known loci

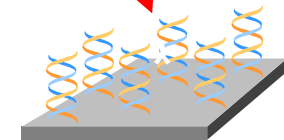
CN locus:

...CGTAGCCATCGGTAAGTACTCAATGATAG...

PM:

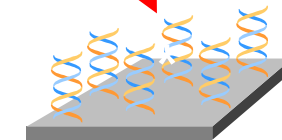
ATCGGTAGCCATTCATGAGTTACTA

CN=1



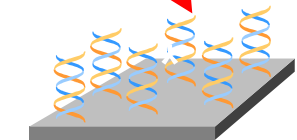
PM = c

CN=2



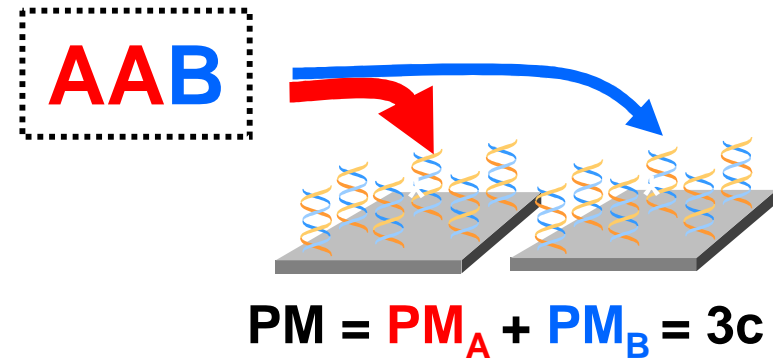
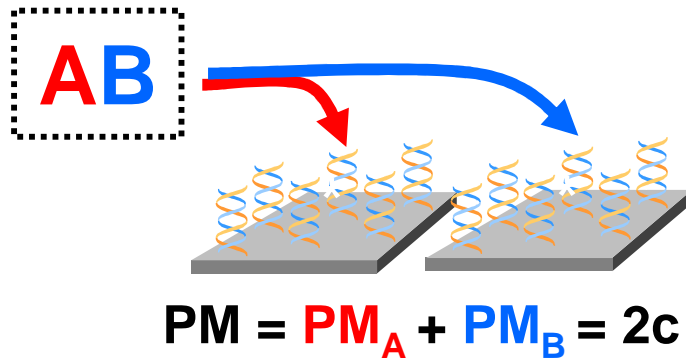
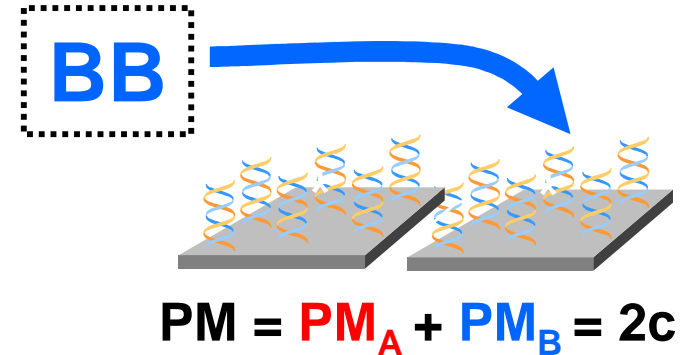
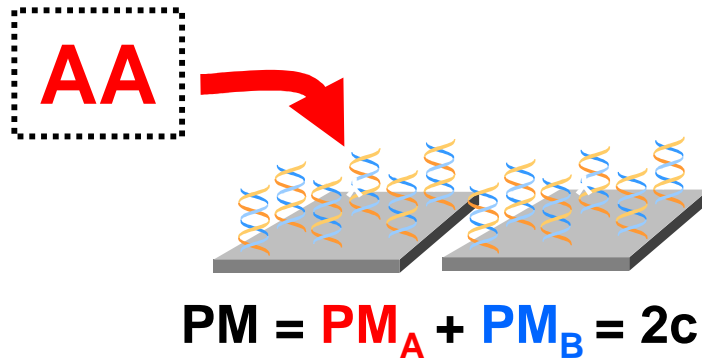
PM = 2c

CN=3



PM = 3c

SNP probes can also be used to estimate total copy numbers



	CRMA v2
Preprocessing (probe signals)	1. Allelic crosstalk calibration 2. Probe-sequence normalization
Summarization	Robust averaging: CN probes: $\theta_{ij} = PM_{ij}$ SNPs: $\theta_{ijA} = \text{median}_k(PM_{ijkA})$ $\theta_{ijB} = \text{median}_k(PM_{ijkB})$ array i , loci j , probe k .
Post-processing	PCR fragment-length normalization
Transform	$(\theta_{ijA}, \theta_{ijB}) \Rightarrow (\theta_{ij}, \beta_{ij})$ $\theta_{ij} = \theta_{ijA} + \theta_{ijB}$, $\beta_{ij} = \theta_{ijB} / \theta_{ij}$
Allele-specific & total CNs	$C_{ijA} = 2^{*(\theta_{ijA} / \theta_{Rj})}$ and $C_{ijB} = 2^{*(\theta_{ijB} / \theta_{Rj})}$ $C_{ij} = 2^{*(\theta_{ij} / \theta_{Rj})}$ reference R

Allelic crosstalk calibration

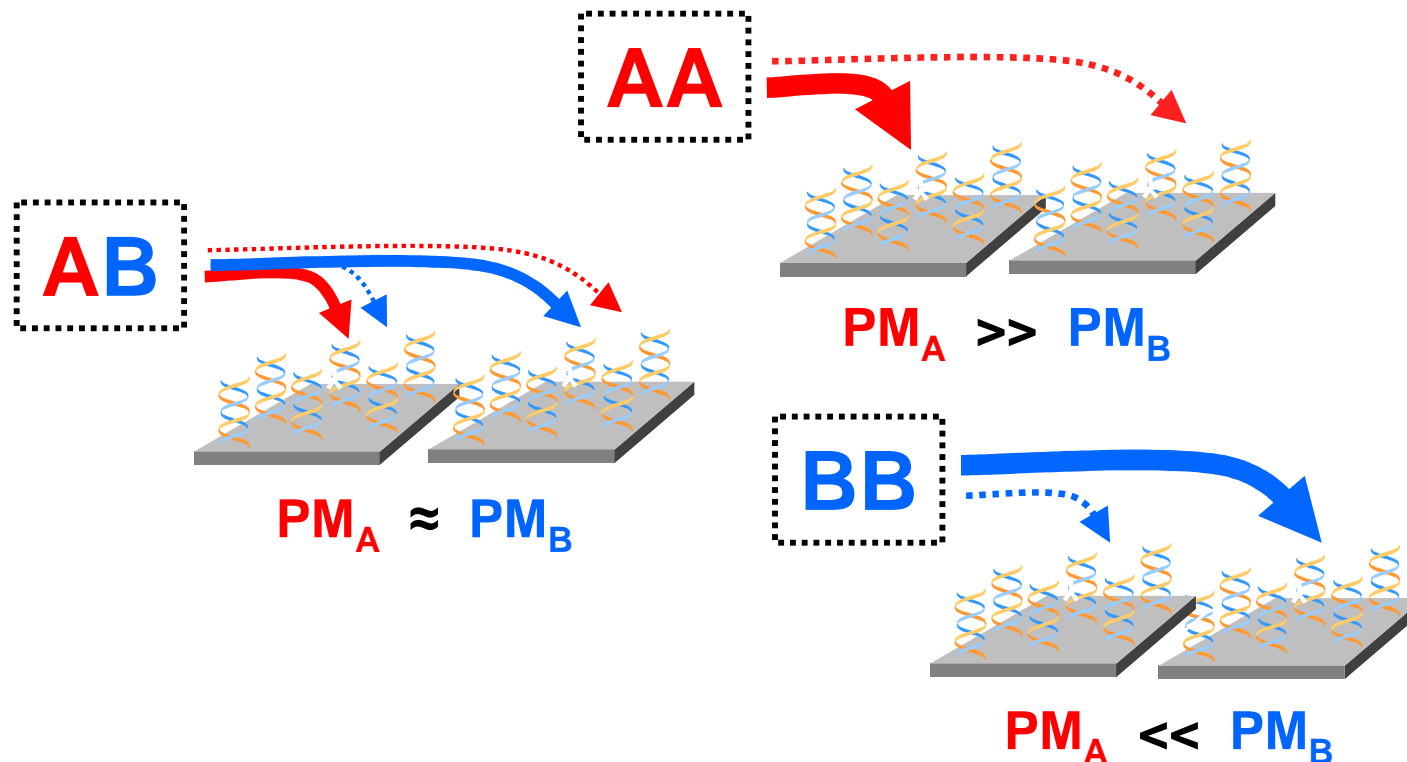
Crosstalk between alleles

- *adds significant artifacts to signals*

Cross-hybridization:

Allele A: TCGGTA**A**GTACTC

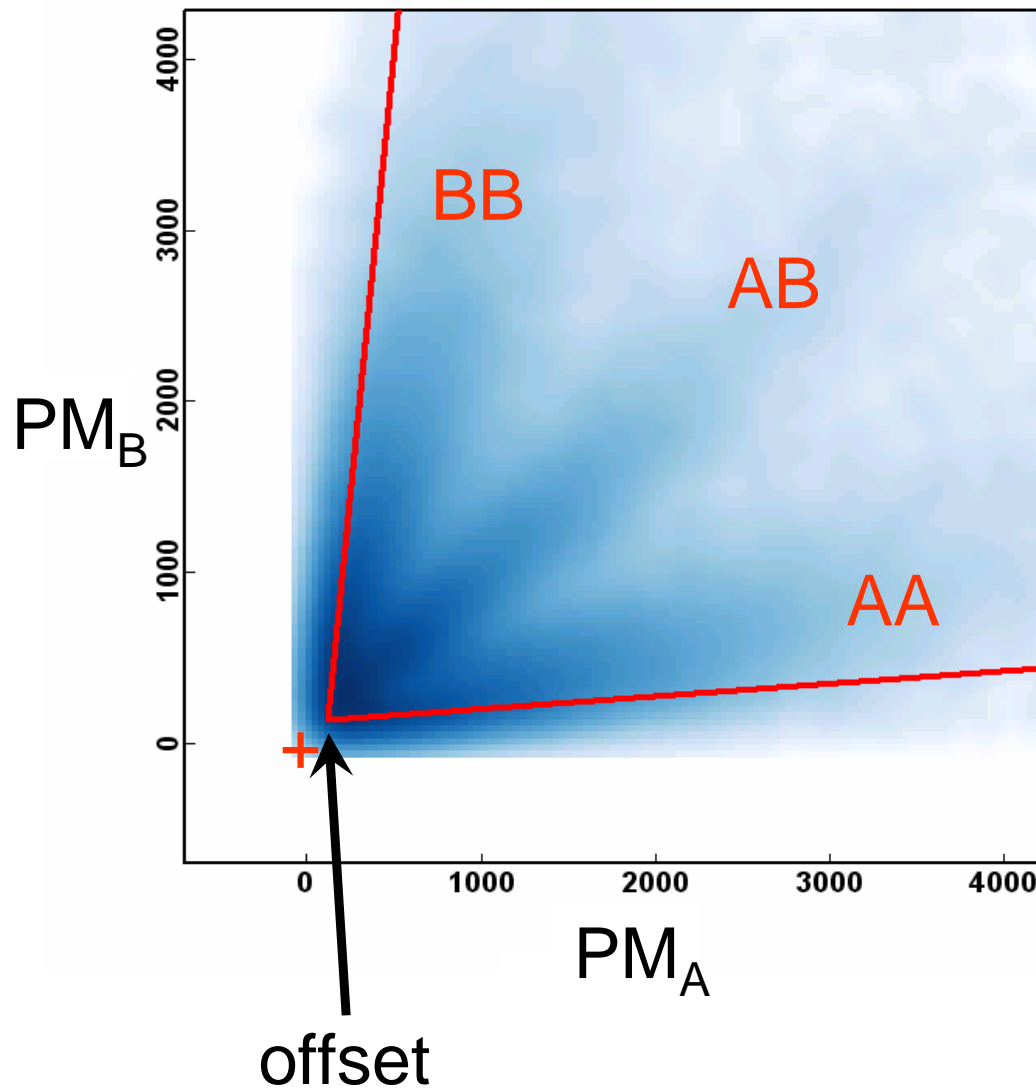
Allele B: TCGGTA**T**GTACTC



There are six possible allele pairs

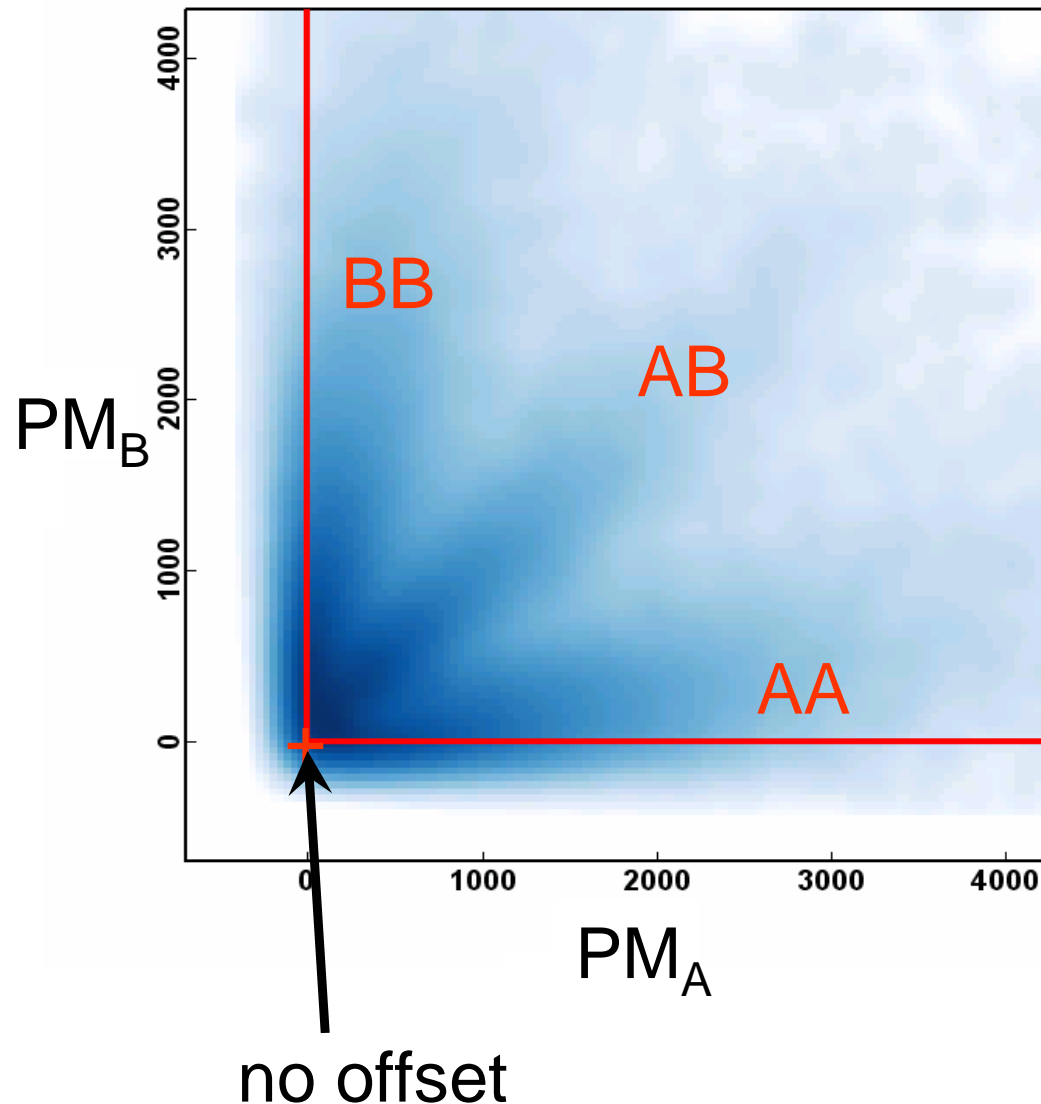
- Nucleotides: {A, C, G, T}
- Ordered pairs:
 - (A,C), (A,G), (A,T), (C,G), (C,T), (G,C)
- Because of different nucleotides bind differently, the crosstalk from A to C might be very different from A to T.

Crosstalk between alleles is easy to spot



Example:
Data from one array.
Probe pairs (PM_A , PM_B)
for nucleotide pair (A,T).

Crosstalk between alleles can be estimated and corrected for



What is done:

1. **Offset is removed** from SNPs and CN units.
2. **Crosstalk is removed** from SNPs.

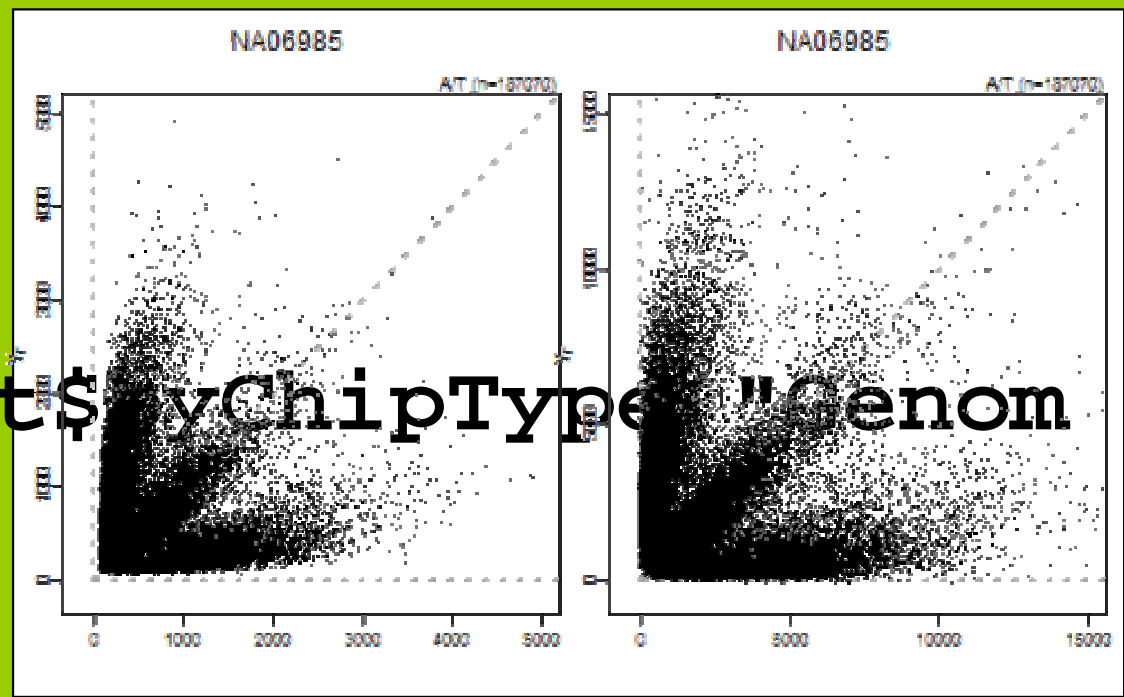
aroma.affymetrix

You will need:

- Affymetrix CDF, e.g. GenomeWideSNP_6.cdf
- Probe sequences*, e.g. GenomeWideSNP_6.acs

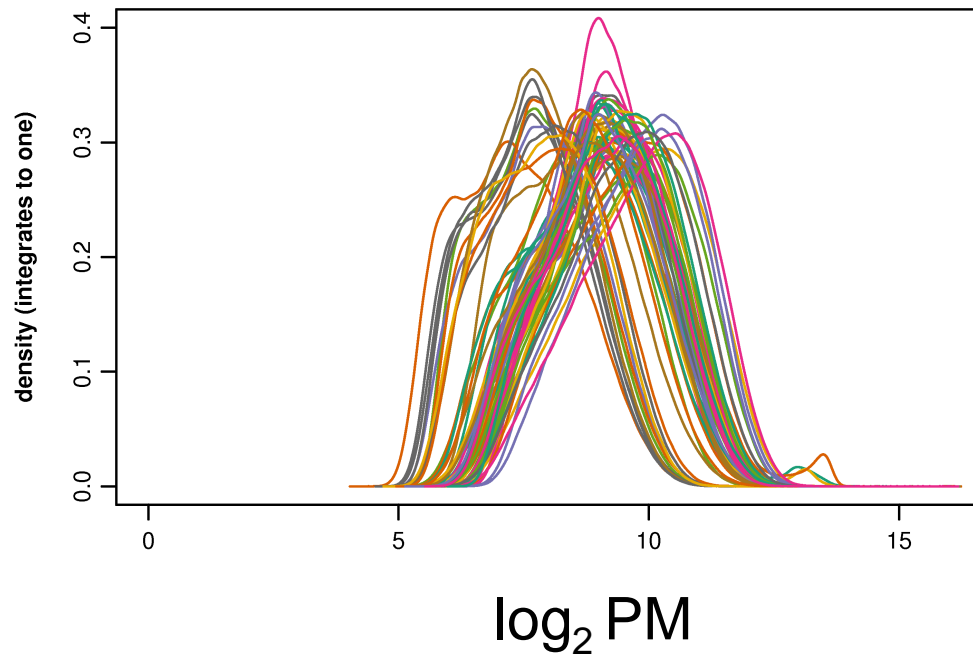
Calibrate CEL files:

```
cdf <-  
  AffymetrixCdfset$myChipType = "Genom  
eWideSNP_6" )  
csR <-
```

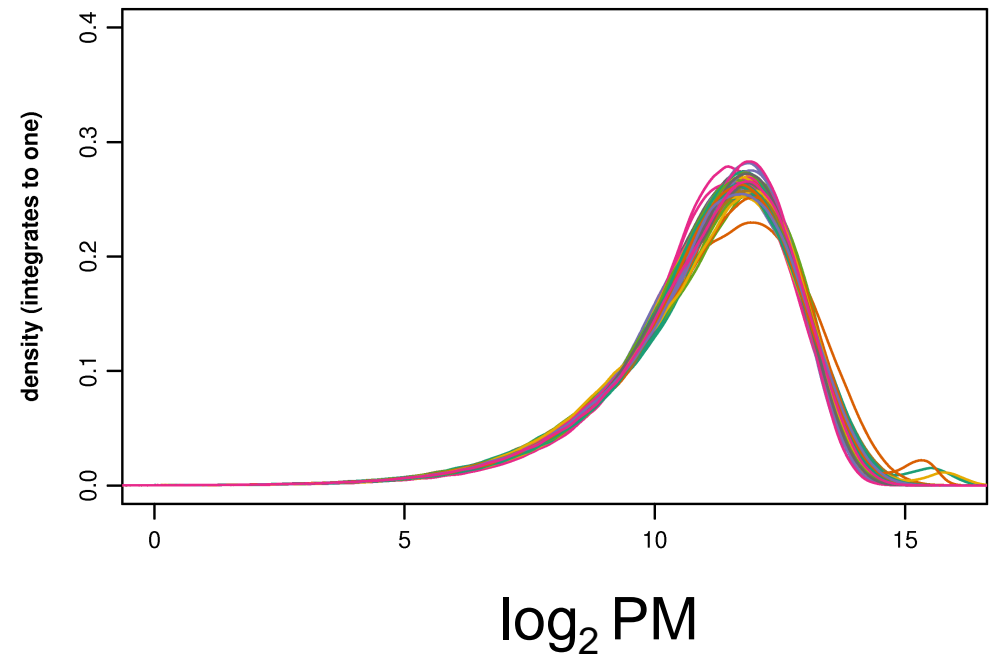


Crosstalk calibration corrects for differences in distributions too

Before removing crosstalk
the arrays differ significantly...



...when removing offset & crosstalk
differences goes away.

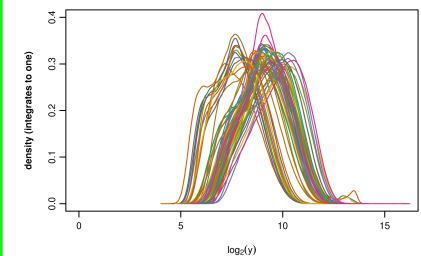
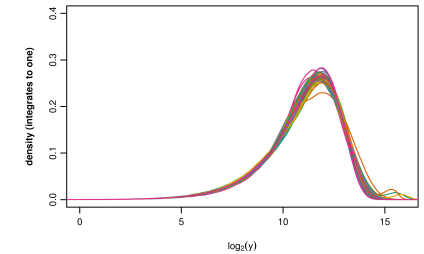
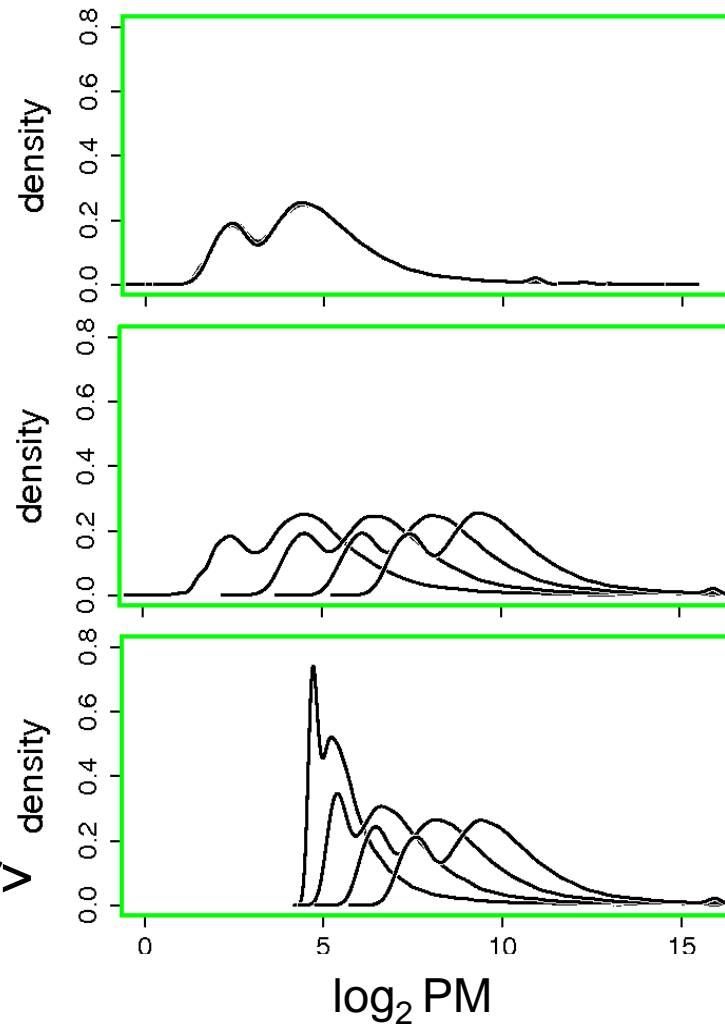


How can a translation and a rescaling make such a big difference?

4 measurements
of the **same thing**:

With **different scales**:
 $\log(b \cdot PM) = \log(b) + \log(PM)$

With **different scales**
and **some offset**:
 $\log(a + b \cdot PM) = \text{non-linear}$



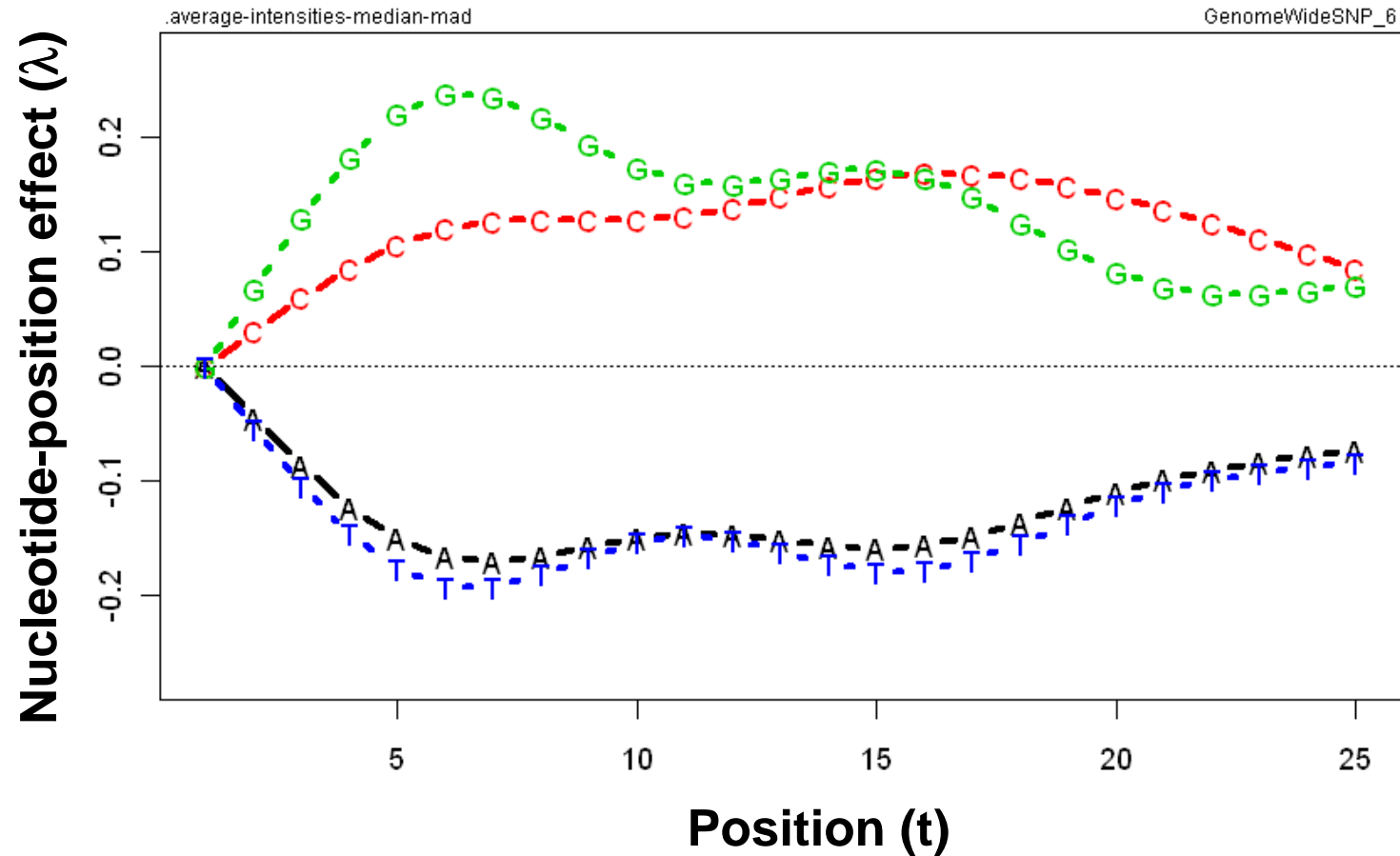
Take home message

Allelic crosstalk calibration controls for:

- 1) offset in signals
- 2) crosstalk between allele A and allele B.

Probe sequence normalization

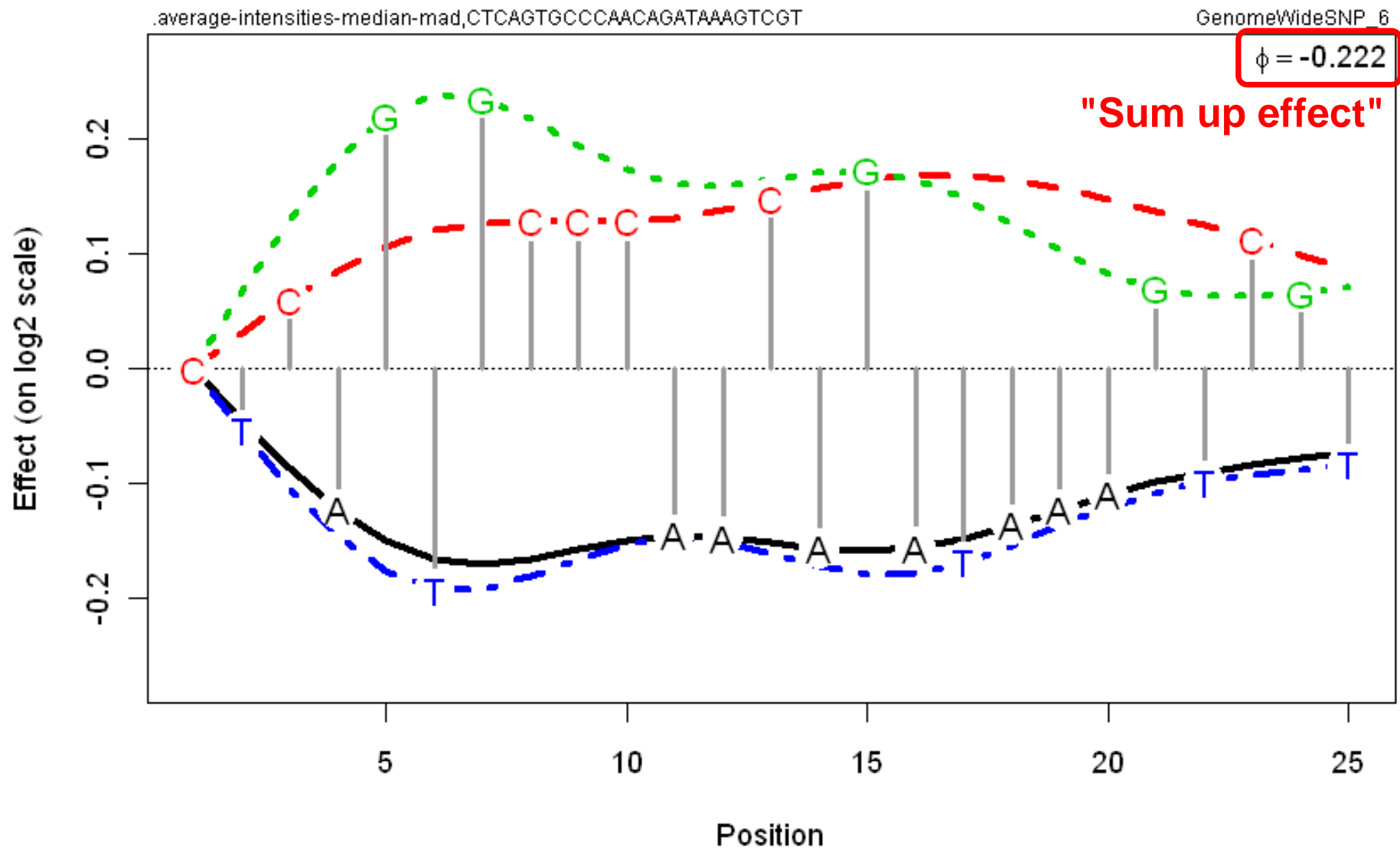
Nucleotide-Position Model



Probe-position (\log_2) affinity for probe k :

$$\phi_k = \phi((b_{k,1}, b_{k,2}, \dots, b_{k,25})) = \sum_{t=1..25} \sum_{b=\{ACGT\}} I(b_{k,t}=b) \lambda_{b,t}$$

Example: Probe-position affinity for CTCAGTGCCCAACAGATAAAAGTCGT



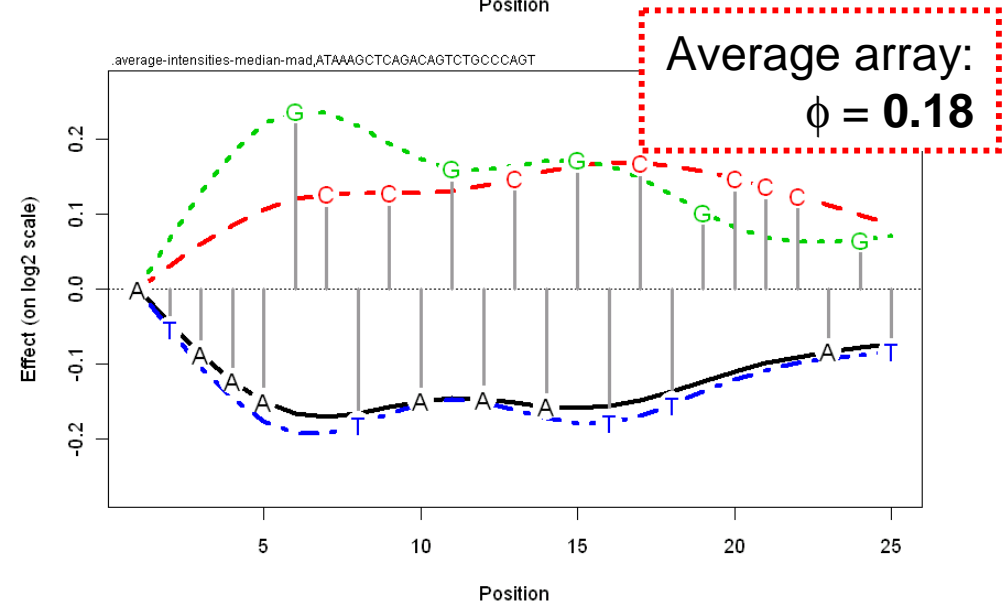
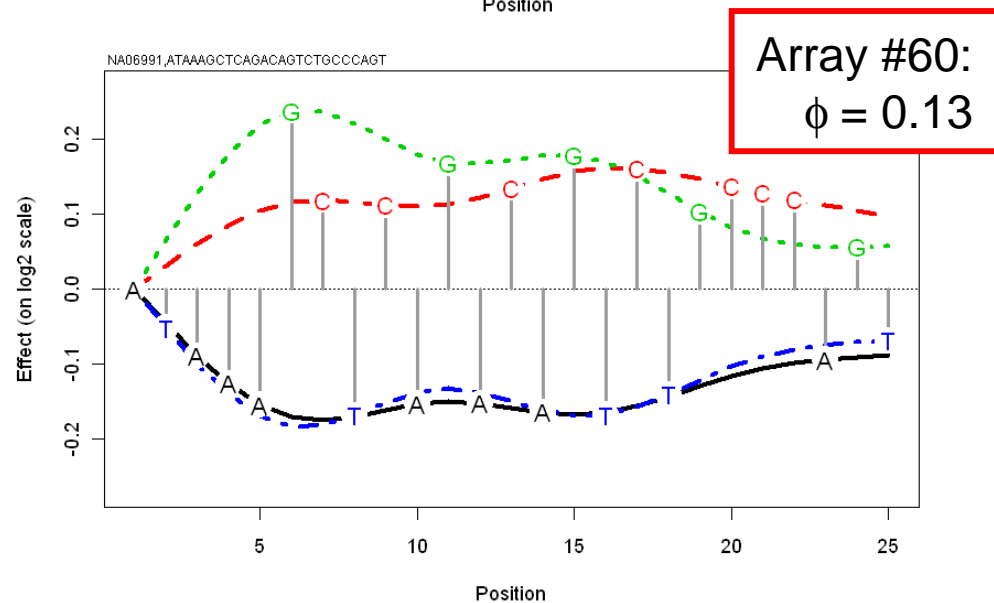
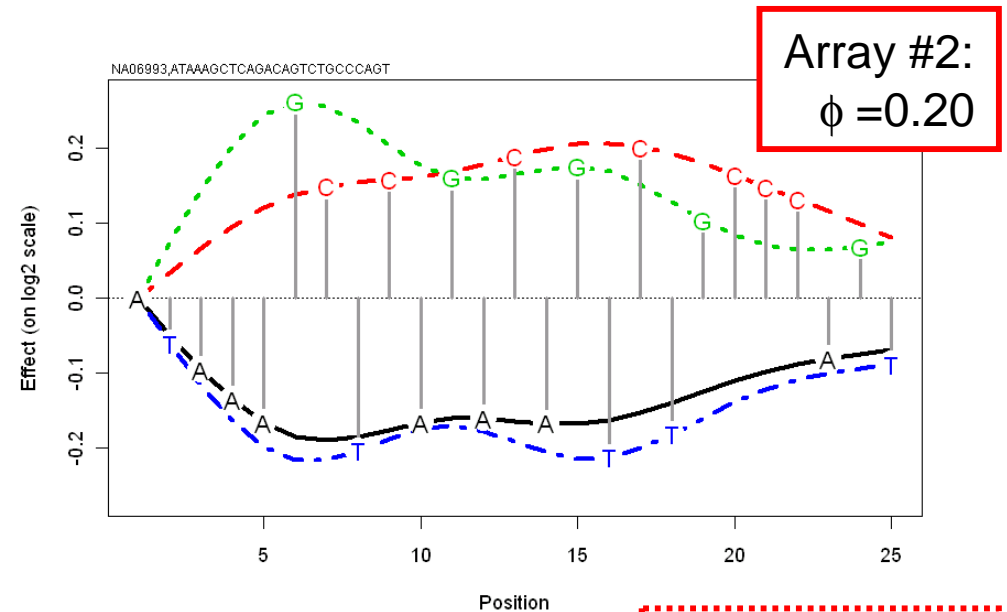
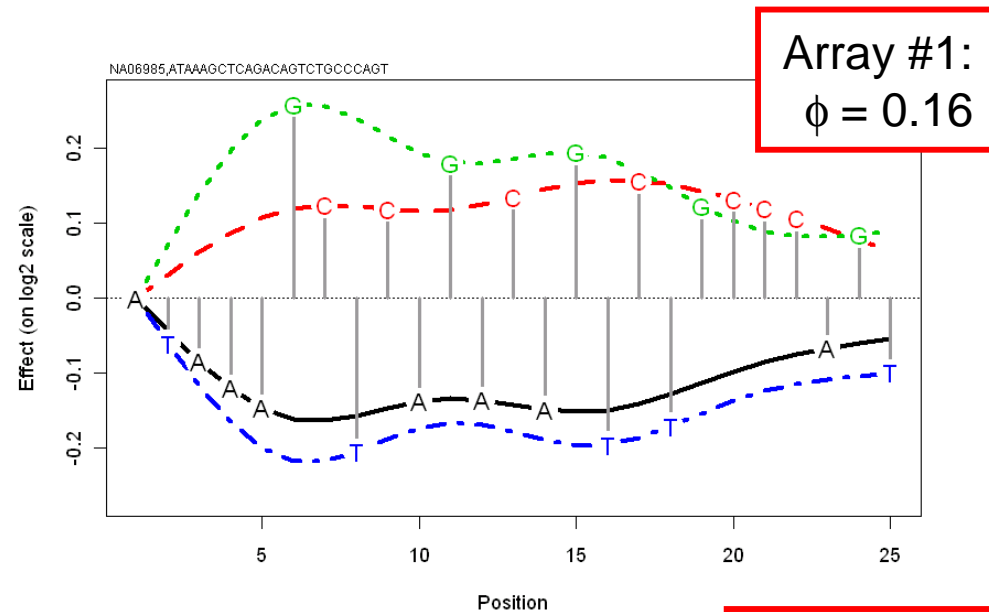
Probe-sequence normalization helps

1. The effects differ slightly across arrays:
 - adds extra across-array variances
 - *will be removed*

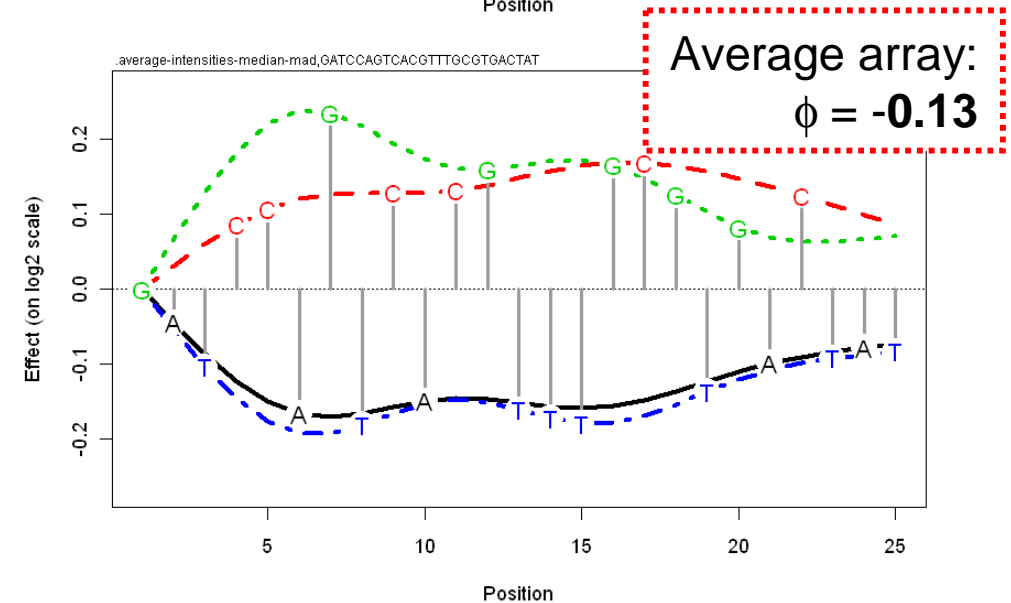
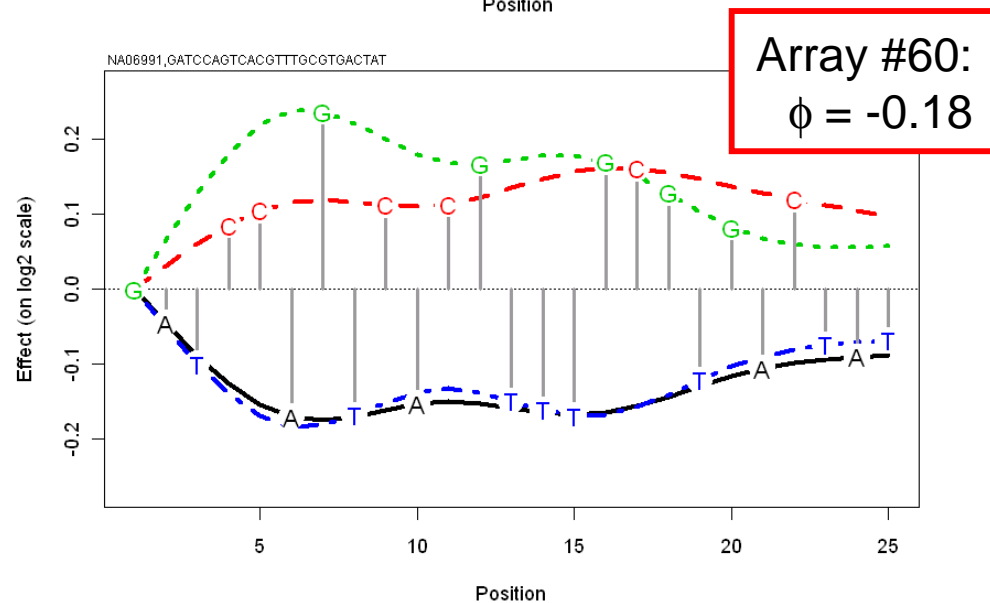
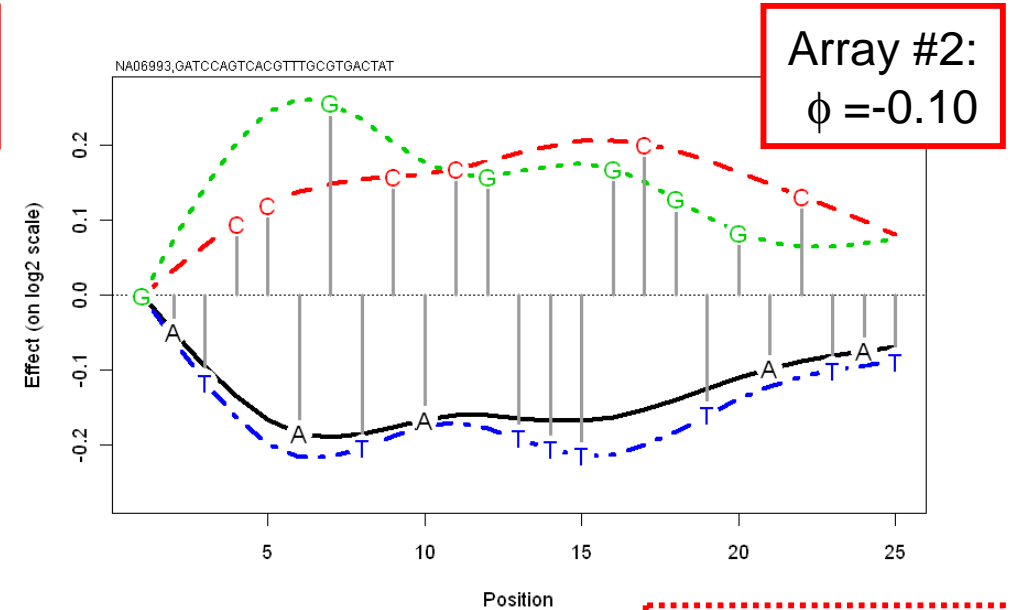
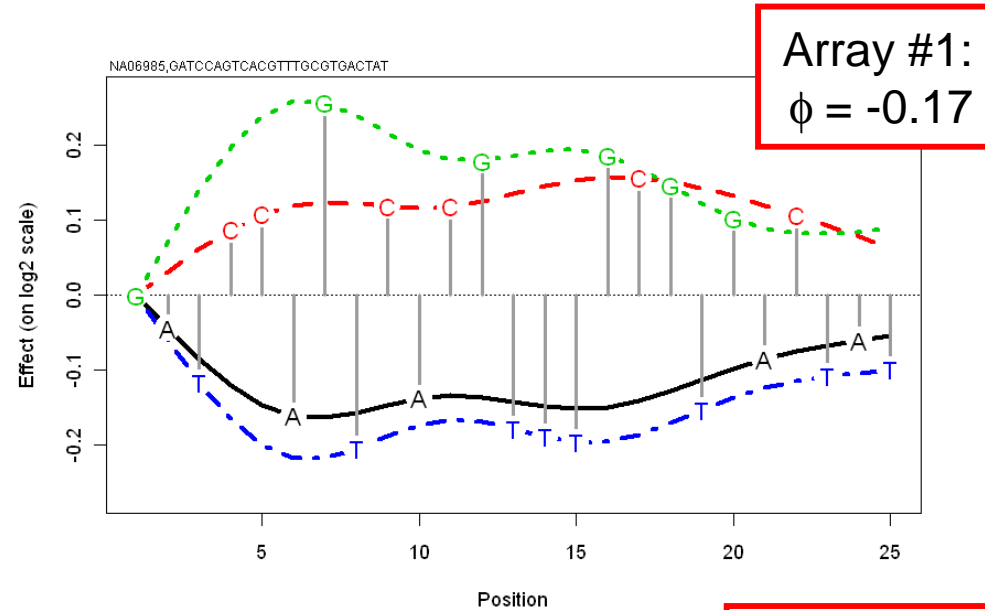
2. The effects differ between PM_A and PM_B :
 - introduces genotypic imbalances such that $PM_A + PM_B$ will differ for AA, AB & BB.
 - *will be removed*

1. BPN controls for across array variability

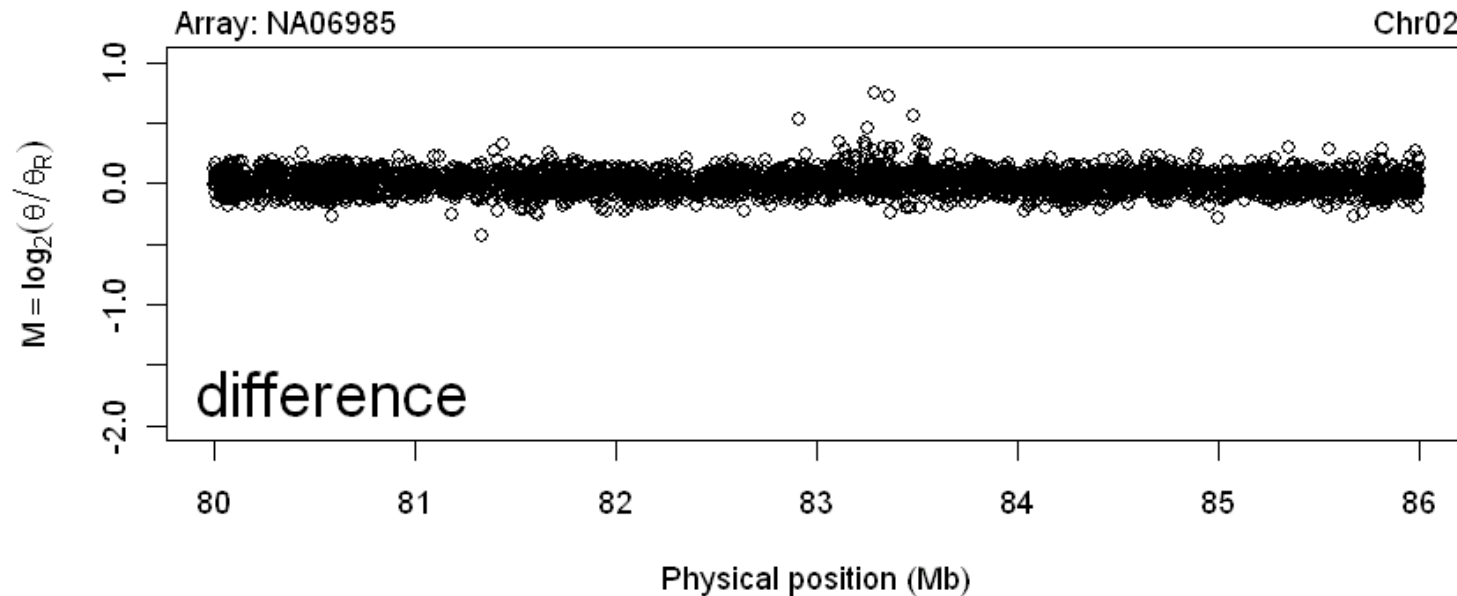
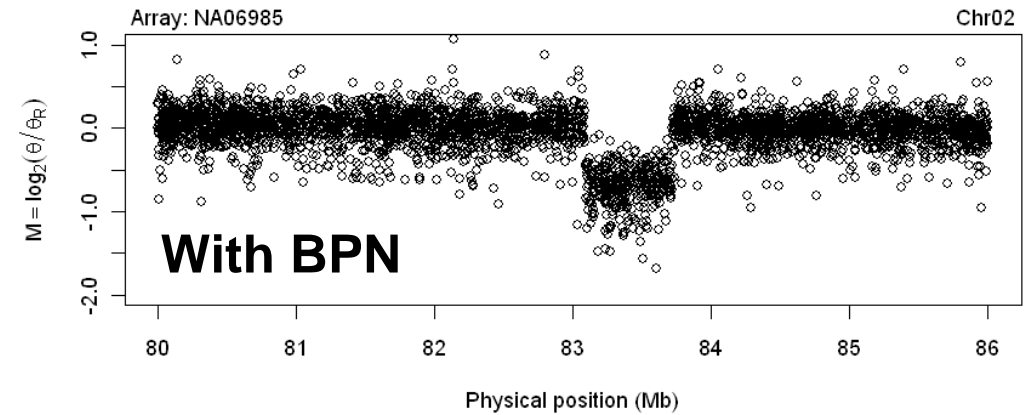
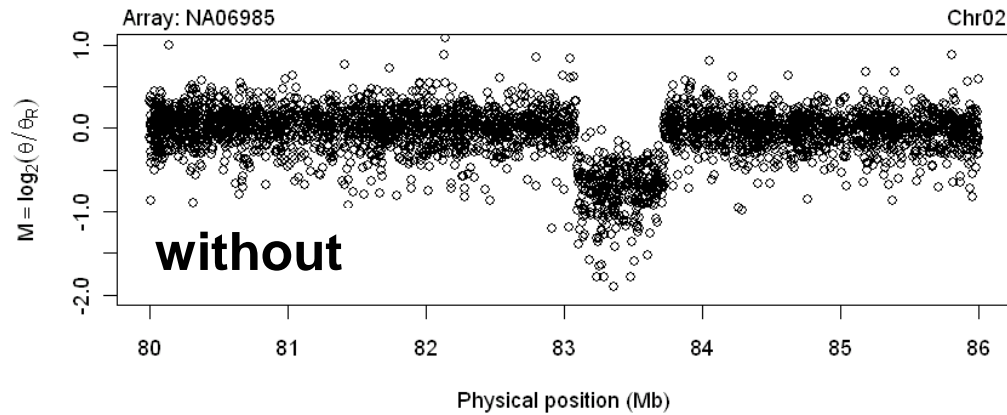
The nucleotide-position effect differ between arrays



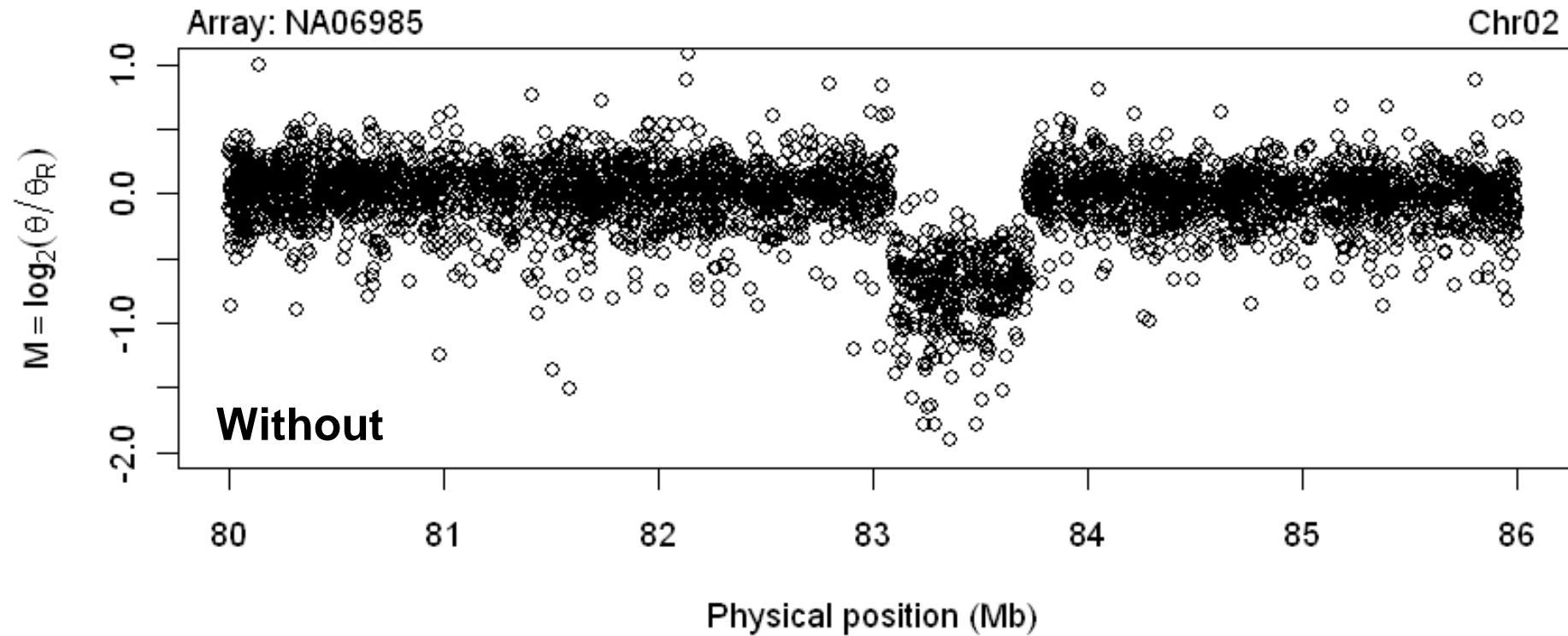
The impact of these effects varies with probe sequence



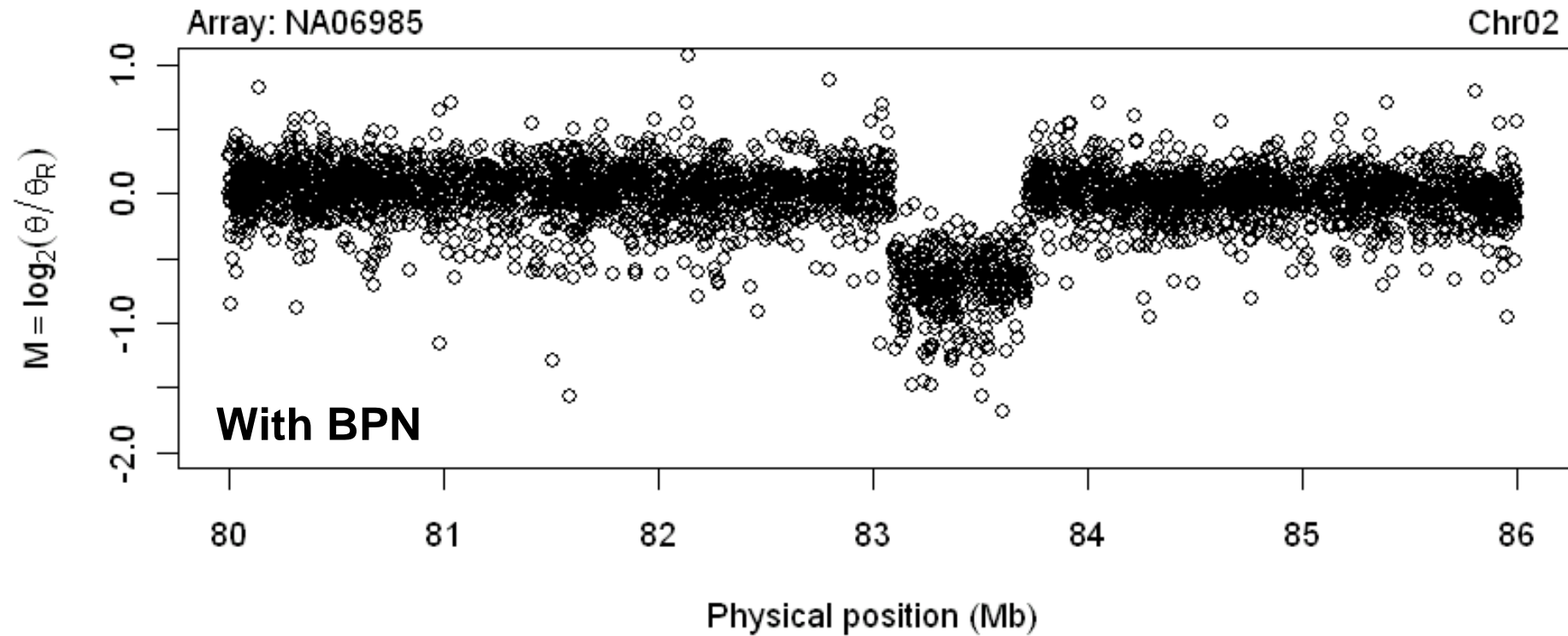
There is a noticeable difference in raw CNs before and after normalization



There is a noticeable difference in raw
CNs before and after normalization

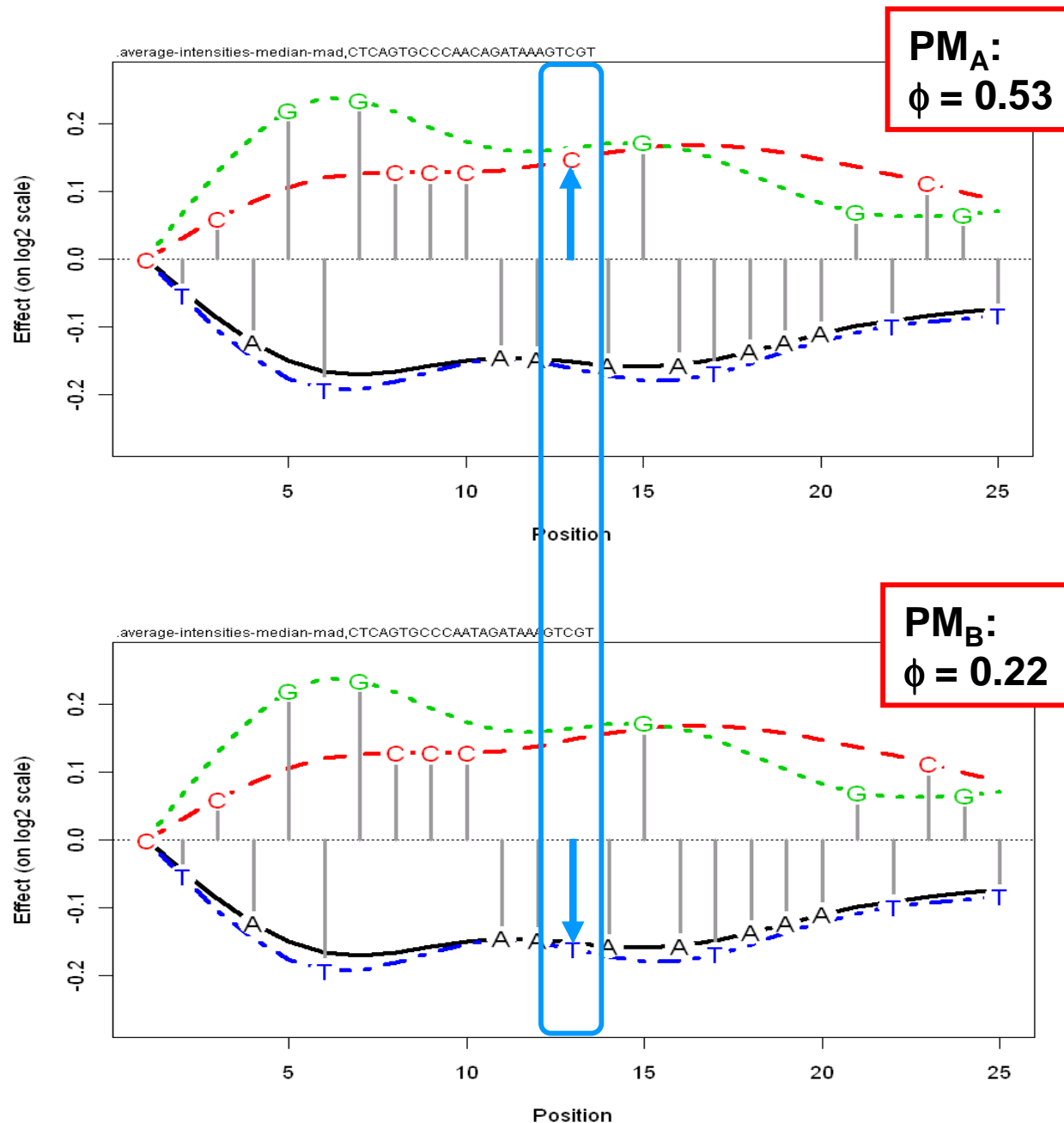


There is a noticeable difference in raw
CNs before and after normalization



2. BPN controls for allele A and allele B imbalances

Nucleotide-position normalization controls for imbalances between allele A & allele B



Genotypic imbalances:

$$PM = PM_A + PM_B:$$

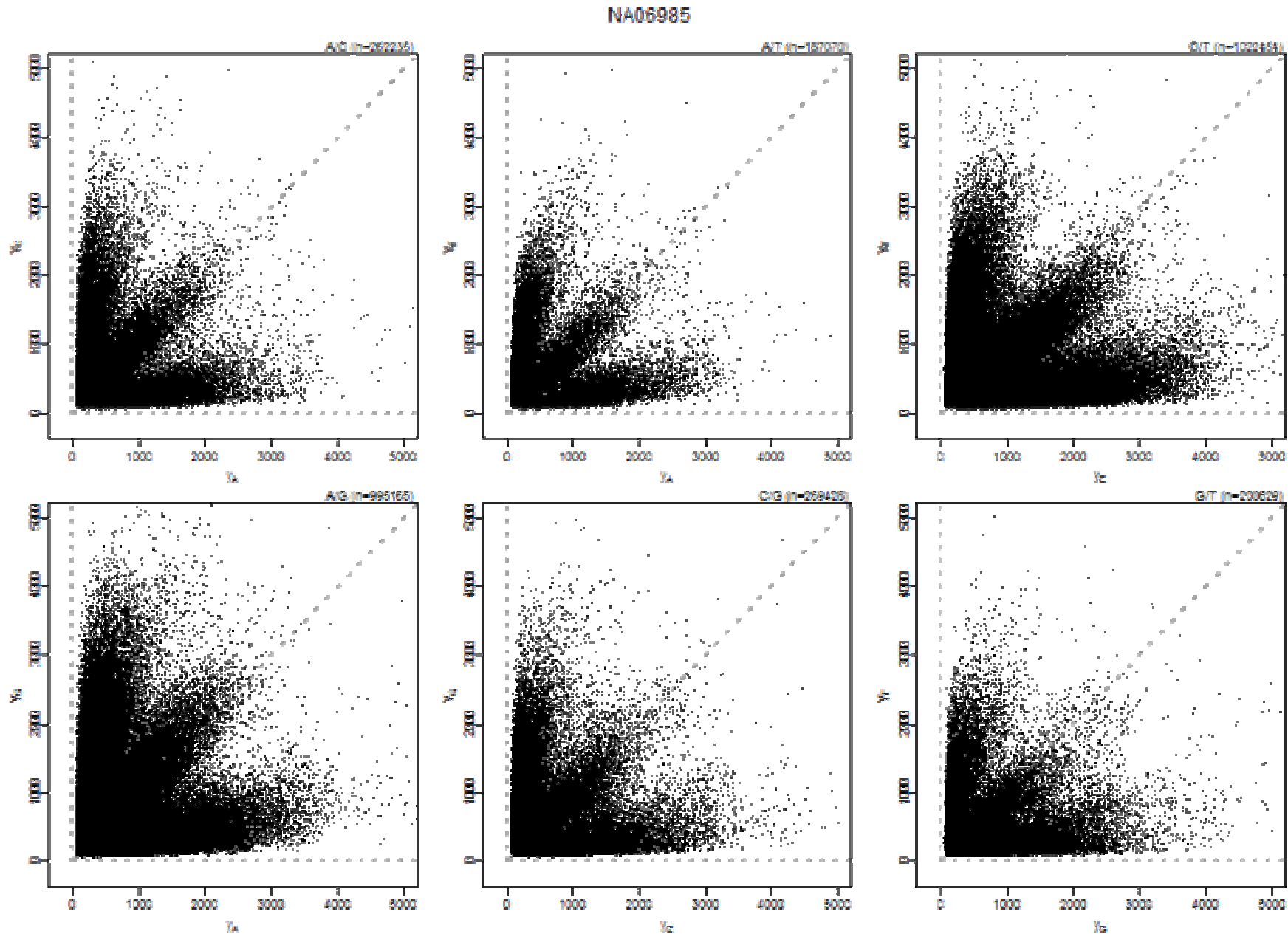
$$AA: 0.53 + 0.53 = 1.06$$

$$AB: 0.53 + 0.22 = 0.75$$

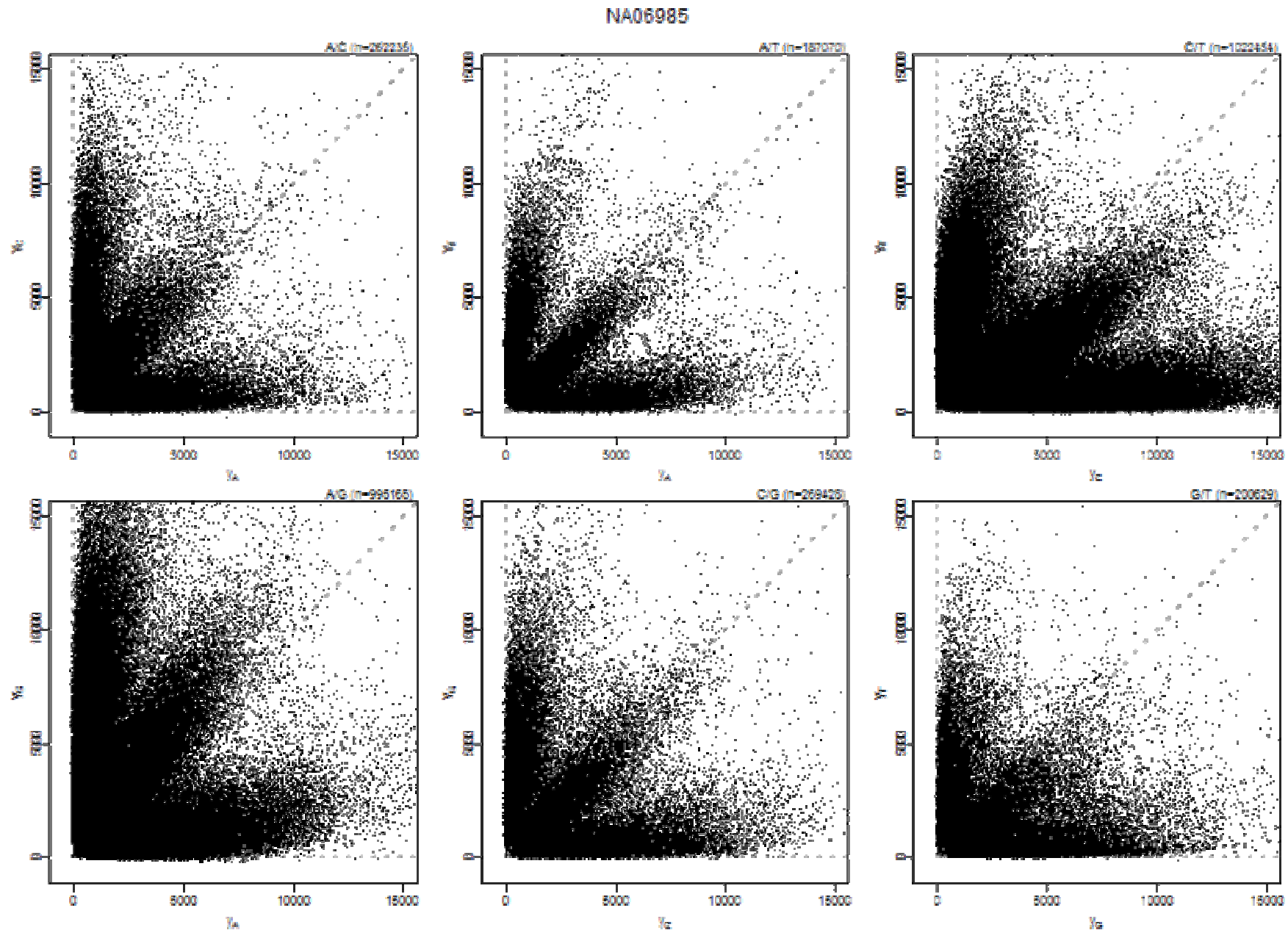
$$BB: 0.22 + 0.22 = 0.44$$

Thus, AA signals are $2^{(1.06-0.44)} = 2^{0.62} = 1.54$ times stronger than BB signals.

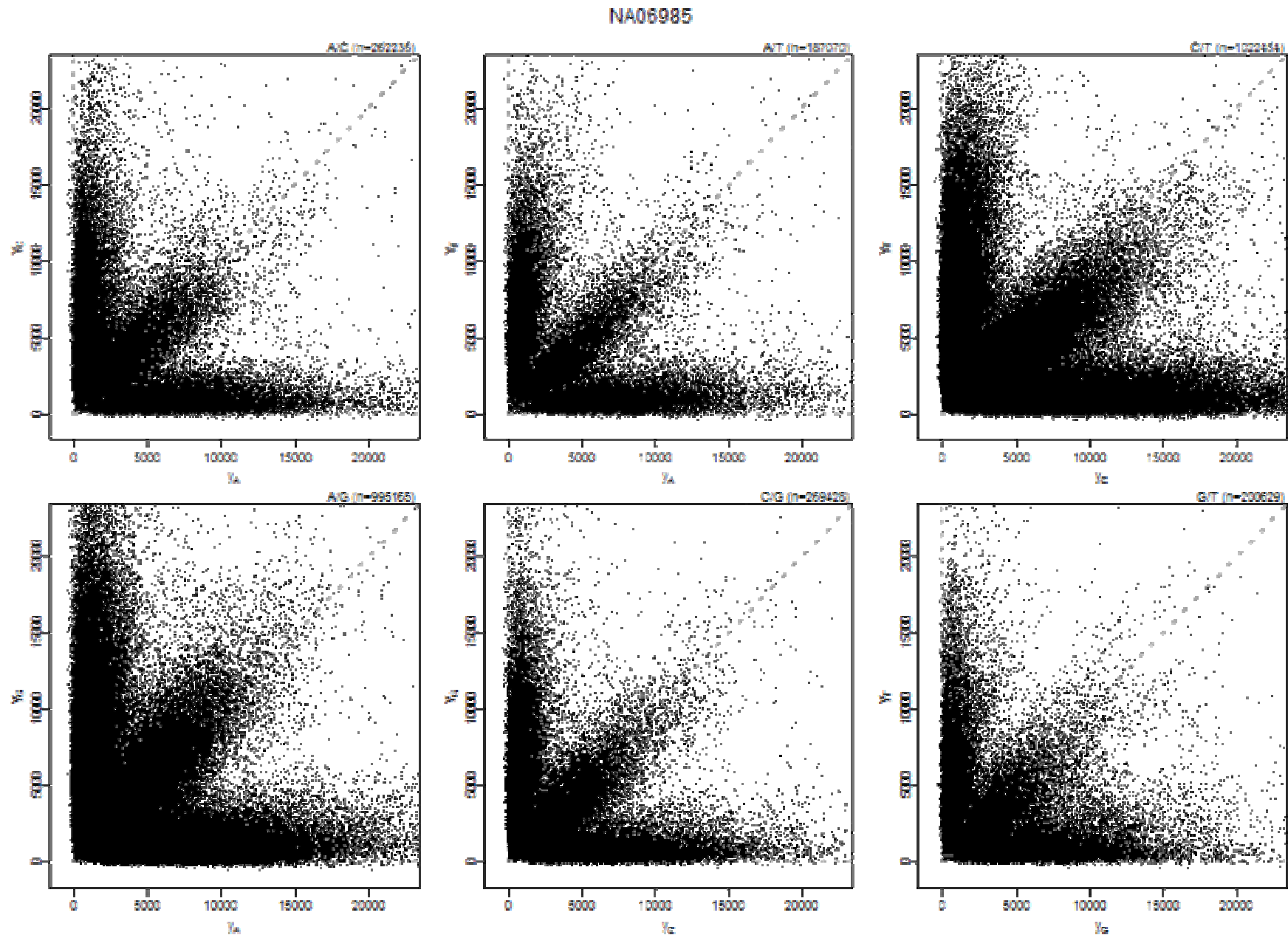
(i) Before calibration there is crosstalk
- *pairs AC, AG, AT, CG, CT & GT*



(ii) After calibration the homozygote arms are more orthogonal (note heterozygote arm!)



(iii) After sequence normalization the heterozygote arms are more balanced



aroma.affymetrix

You will need:

- Affymetrix CDF, e.g. GenomeWideSNP_6.cdf
- Probe sequences*, e.g. GenomeWideSNP_6.acs

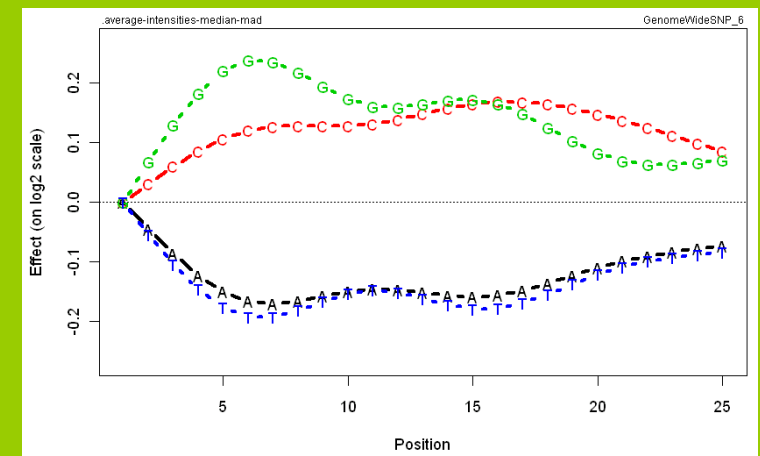
Normalize CEL files:

```
bpn <- BasePositionNormalization(csC, target="zero")  
csN <- process(bpn)
```

Works with any chip type, e.g. resequencing,
exon, expression, SNP.

To plot:

```
fit <- getFit(bpn, array=1)  
plot(fit)
```



Probe summarization

Probe summarization (on the new arrays)

- CN units: All single-probe units:
 - Chip-effect estimate: $\theta_{ij} = PM_{ij}$
- SNPs: Identically replicated probe pairs:
 - Probe pairs: (PM_{ijkA}, PM_{ijkB}) ; $k=1,2,3$
 - Allele-specific estimates:
 - $\theta_{ijA} = \text{median}_k\{PM_{ijkA}\}$
 - $\theta_{ijB} = \text{median}_k\{PM_{ijkB}\}$

aroma.affymetrix

You will need:

- Affymetrix CDF, e.g. GenomeWideSNP_6.cdf

Summarizing probe signals:

```
plm <- AvgCnPlm(csN, combineAlleles=FALSE)
fit(plm)
```

```
ces <- getChipEffectSet(plm)
theta <- extractTheta(ces)
```


Probe-level summarization (10K-500K)

- *(if) replicated probes respond differently*

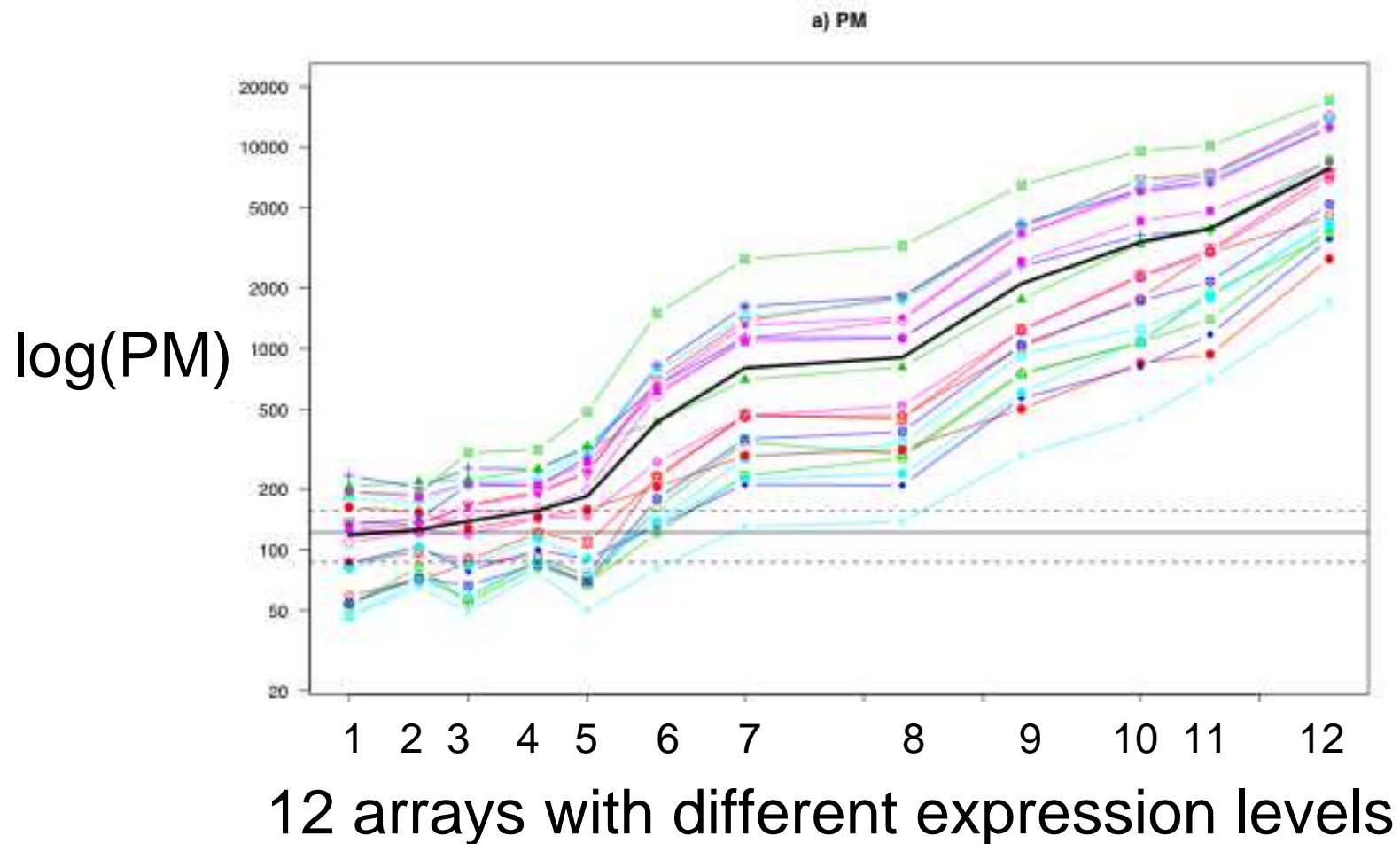
For a particular SNP we now have K added signals:

$$(PM_1, PM_2, \dots, PM_K)$$

which are measures of the same thing - the CN. However, they have slightly different sequences, so their hybridization efficiency might differ.

Probe-level summarization

- different probes respond differently



18 probes
for the same
probe set

Example:

$$\log_2(PM_1) = \log_2(PM_2) + a_1$$

=>

$$PM_1 = \phi_1 * PM_2$$

$(\phi_1 = 2^{a_1})$

Probe-level summarization

- probe affinity model

For a particular SNP, the total CN signal
for sample $i=1,2,\dots,I$ is:

$$\theta_i$$

Which we observe via K probe signals: $(PM_{i1}, PM_{i2}, \dots, PM_{iK})$

rescaled by probe affinities:

$$(\phi_1, \phi_2, \dots, \phi_K)$$

A multiplicative model for the observed PM signals is then:

$$PM_{ik} = \phi_k * \theta_i + \xi_{ik}$$

where ξ_{ik} is noise.

Probe-level summarization

- *the log-additive model*

For one SNP, the model is:

$$PM_{ik} = \phi_k * \theta_i + \xi_{ik}$$

Take the logarithm on both sides:

$$\begin{aligned}\log_2(PM_{ik}) &= \log_2(\phi_k * \theta_i + \xi_{ik}) \\ &\approx \log_2(\phi_k * \theta_i) + \frac{1}{4} \xi_{ik} \\ &= \log_2 \phi_k + \log_2 \theta_i + \varepsilon_{ik}\end{aligned}$$

Sample $i=1,2,\dots,I$, and probe $k=1,2,\dots,K$.

Probe-level summarization

- the log-additive model

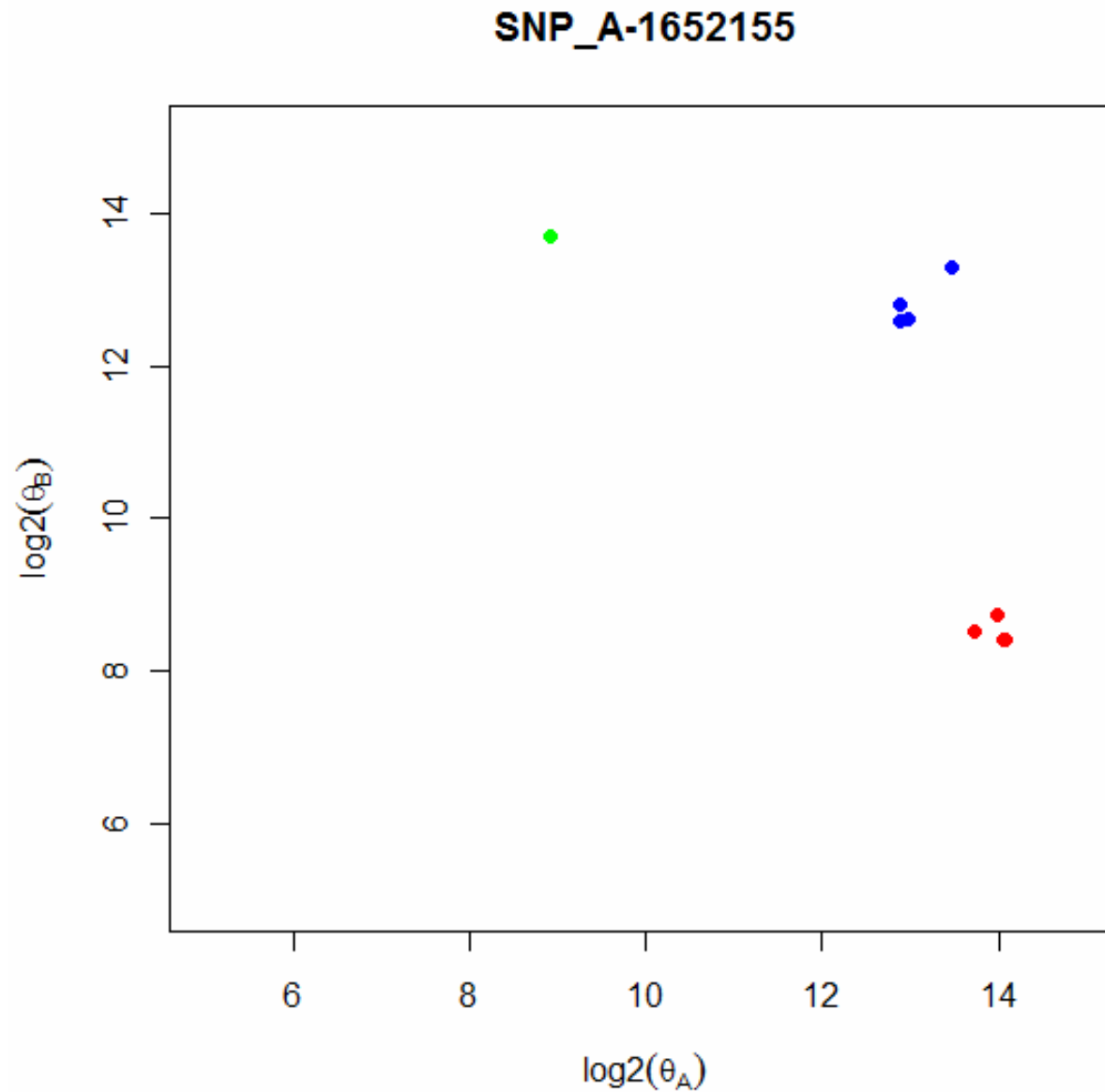
With multiple arrays $i=1,2,\dots,I$, we can estimate the probe-affinity parameters $\{\phi_k\}$ and therefore also the "chip effects" $\{\theta_i\}$ in the model:

$$\log_2(\text{PM}_{ik}) = \log_2\phi_k + \log_2\theta_i + \varepsilon_{ik}$$

Conclusion: We have summarized signals $(\text{PM}_{Ak}, \text{PM}_{Bk})$ for probes $k=1,2,\dots,K$ into **one signal θ_i per sample.**

Very brief on existing genotyping algorithms

Allele-specific estimates ($\theta_{ijA}, \theta_{ijB}$)



Idea of RLMM, BRLMM, CRLMM

Find genotype regions for each SNP:

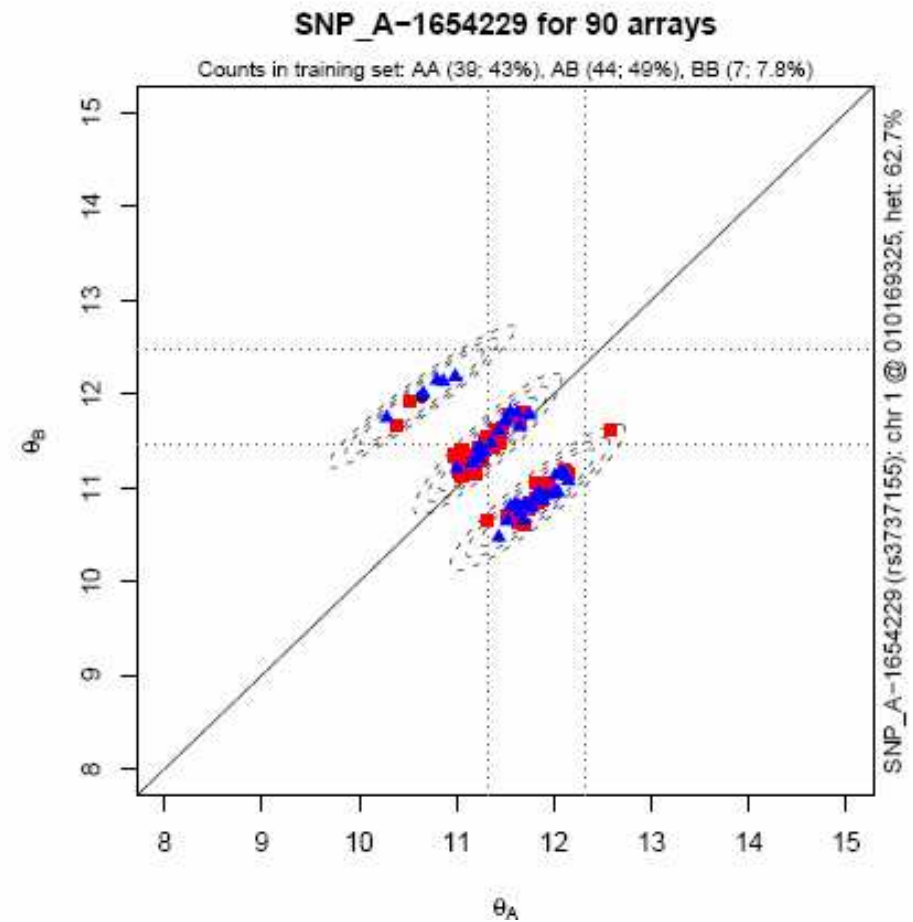
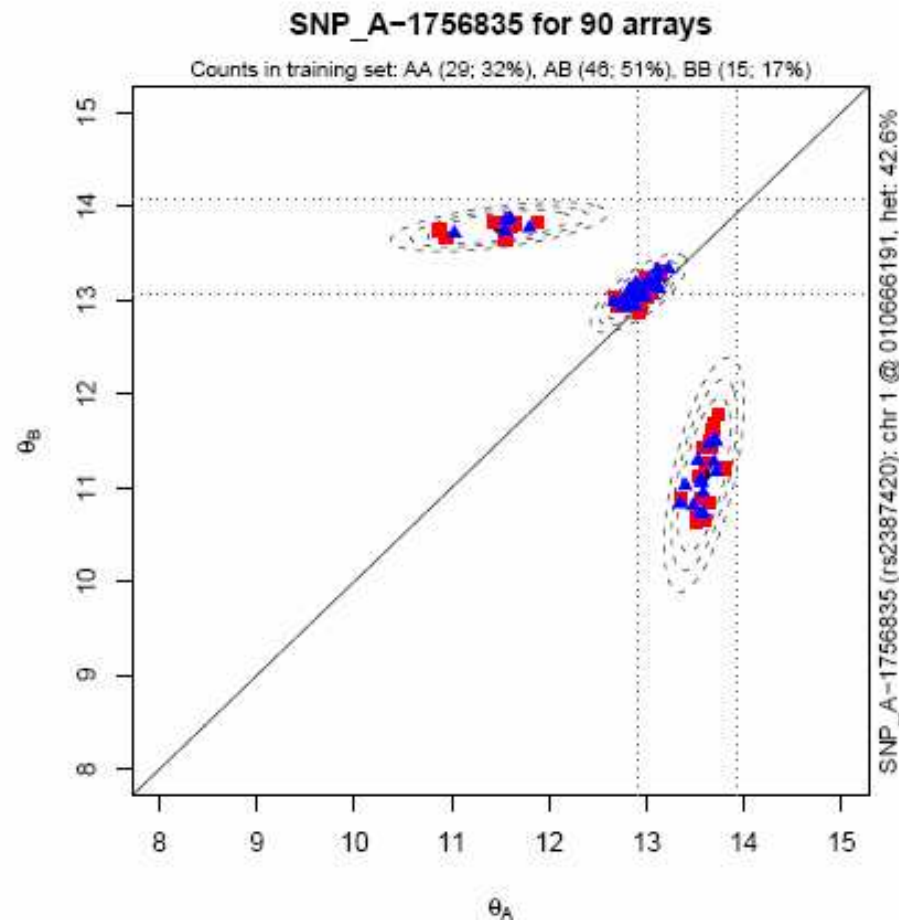
- Pick a high-quality training data set for which we know the true genotypes, e.g. the 270 HapMap samples.
- Estimate $(\theta_{ijA}, \theta_{ijB})$ for all samples and SNPs.
- For each SNP, find the regions for all samples with AA, then with AB, and the with BB.
 - The regions will differ slightly between SNPs.
- (Bayesian modelling of prior SNP regions)

For a new sample:

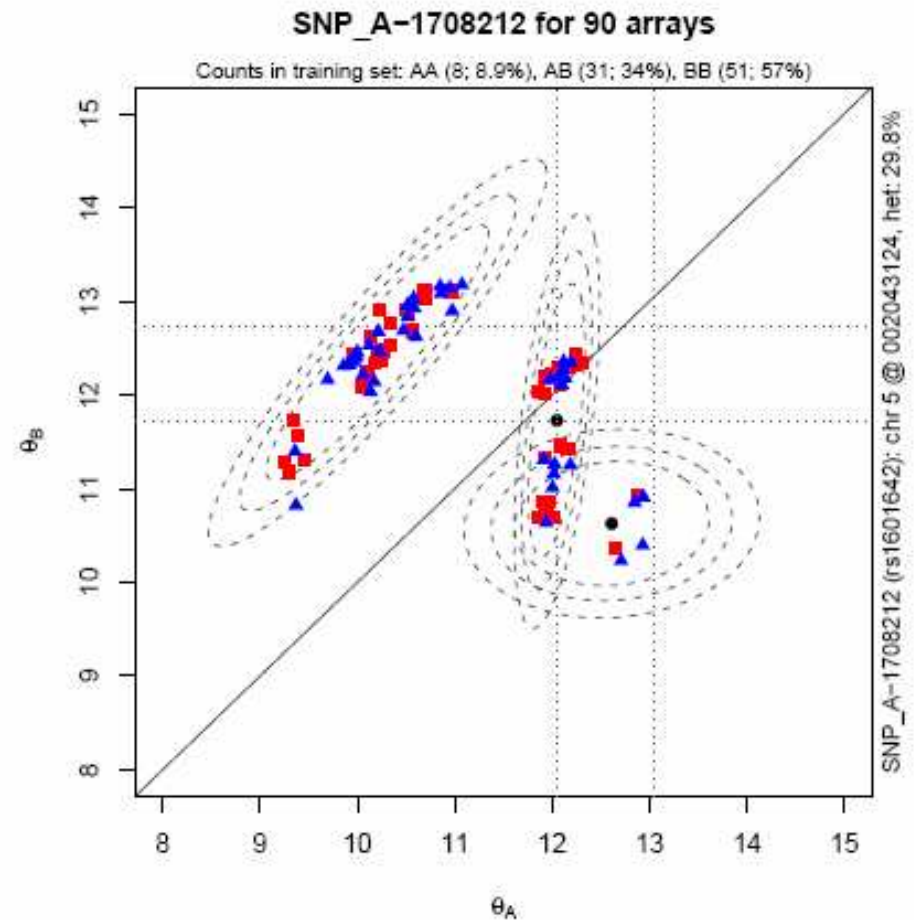
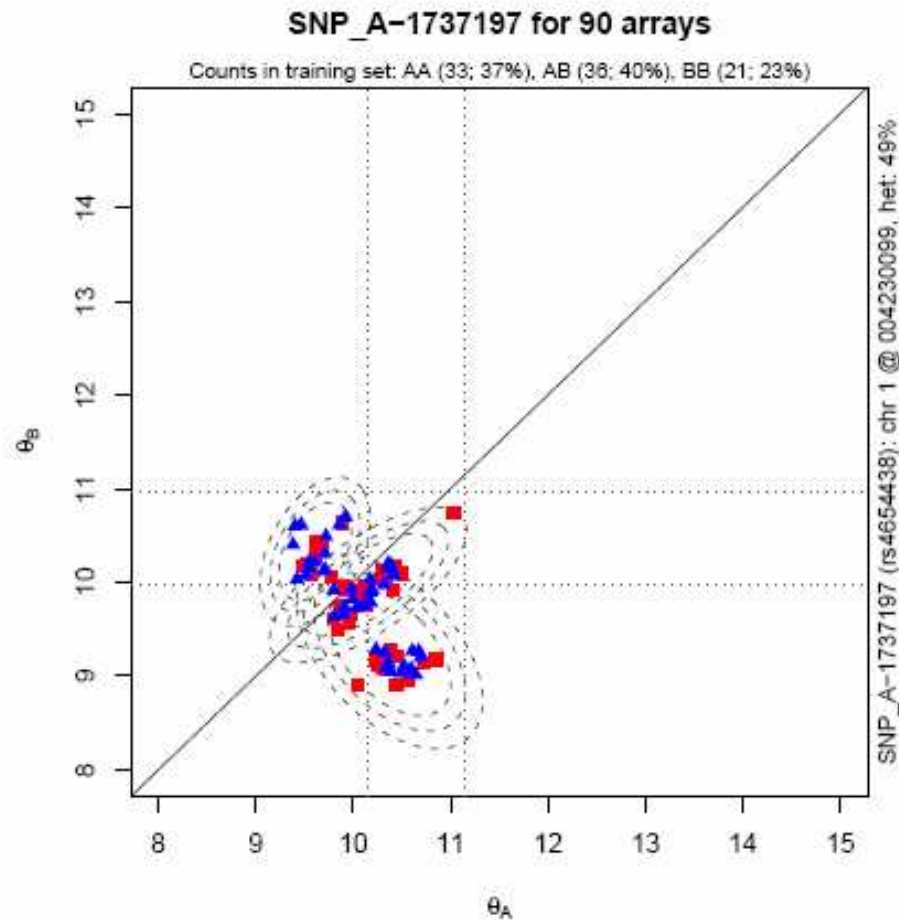
- For each SNP, identify the trained genotype region that is closest to its $(\theta_{ijA}, \theta_{ijB})$. That will be the genotype.

Calling genotyping in $(\theta_{ijA}, \theta_{ijB})$

Example: Two SNPs on chromosome 1

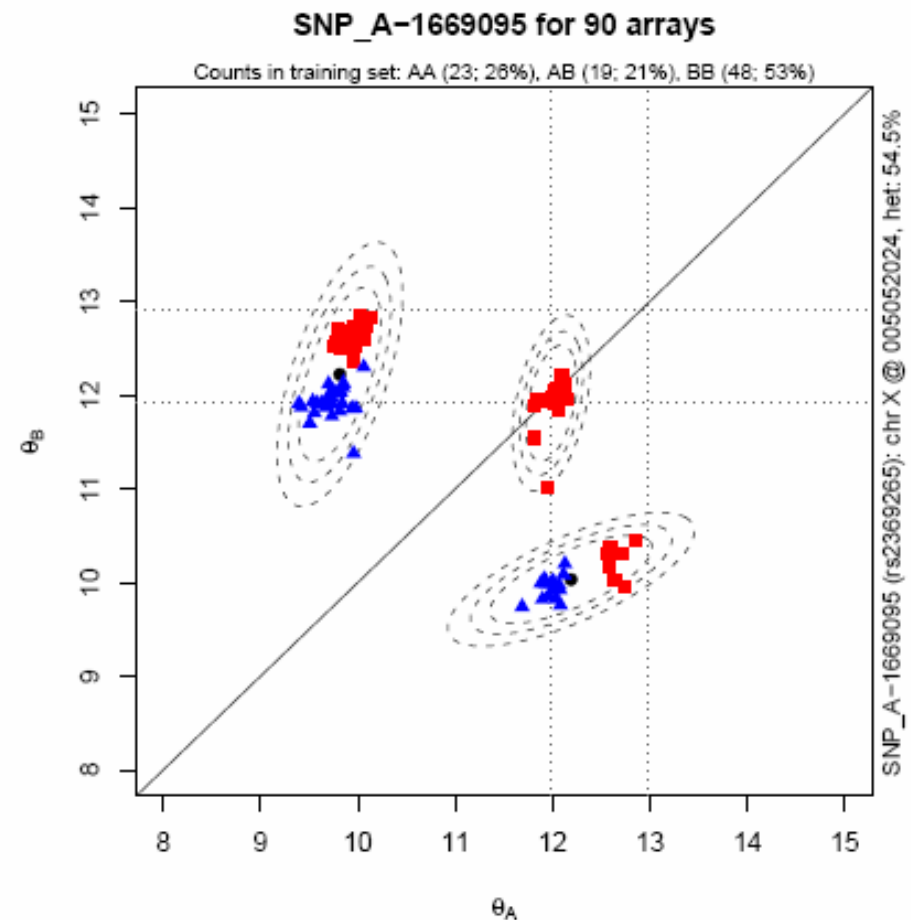
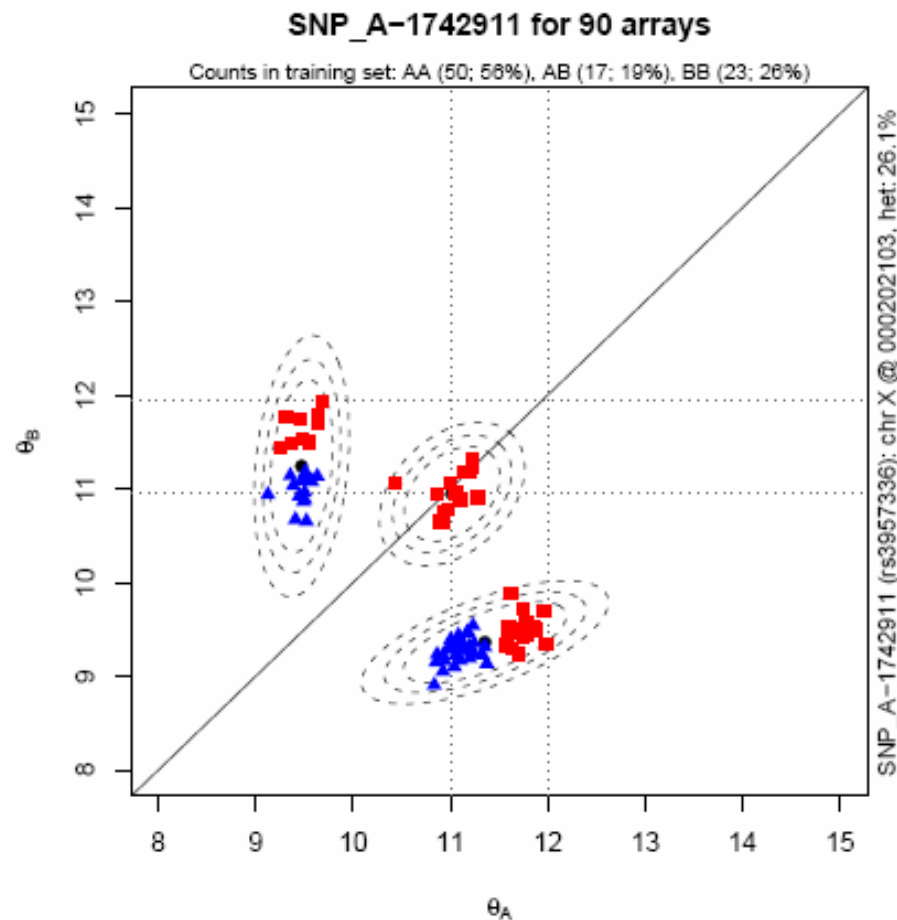


For some SNPs it is harder to distinguish the genotype groups



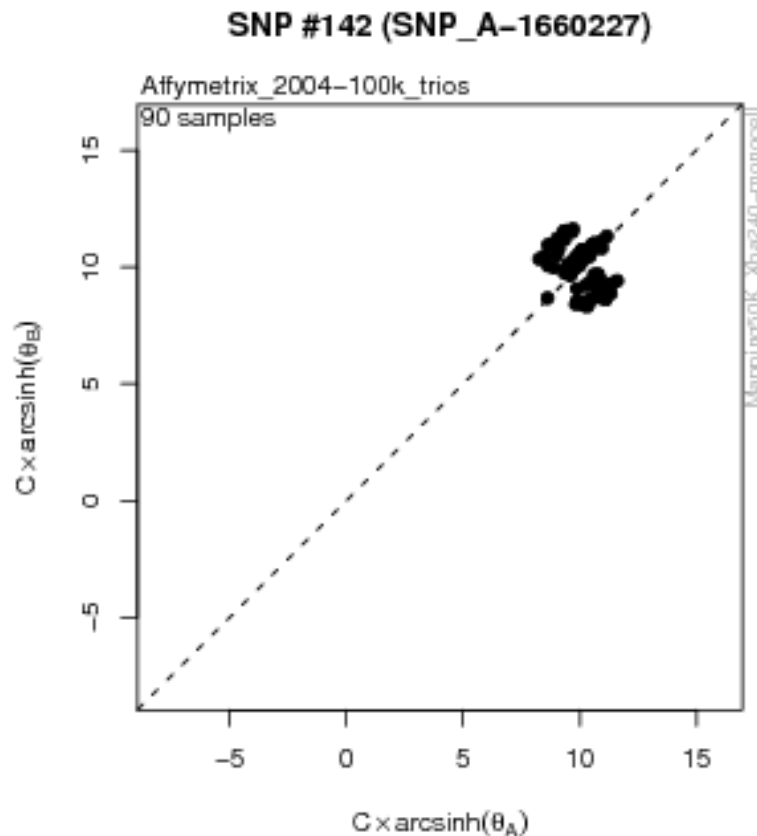
Careful: Genotyping algorithms often assume diploid states, not CN aberrations

Example: Two SNPs on chromosome X

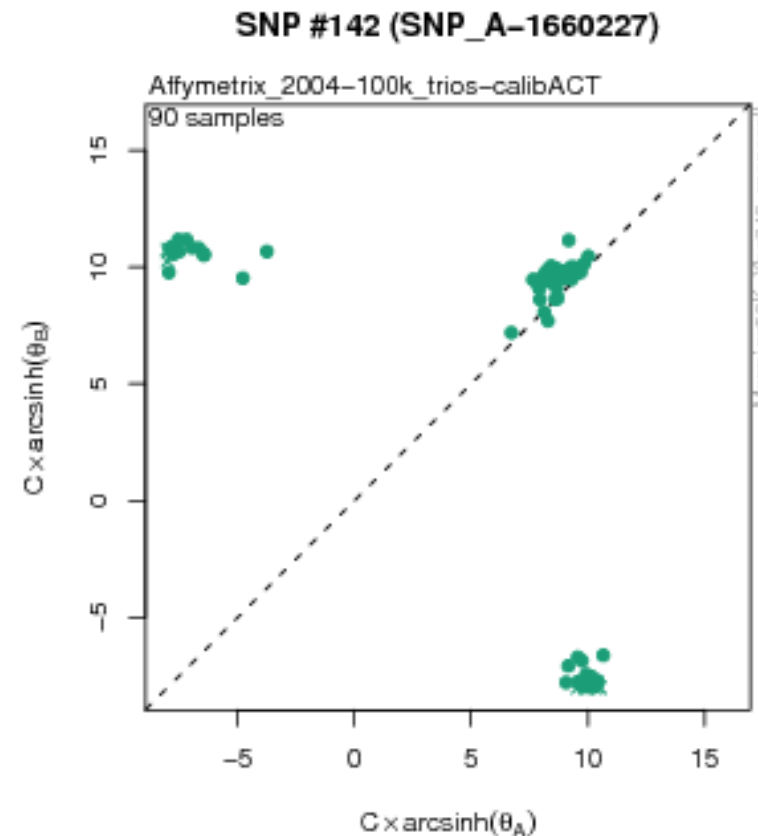


Crosstalk calibration (incl. the removal of the offset) gives better separation of AA, AB, BB.

Without calibration:

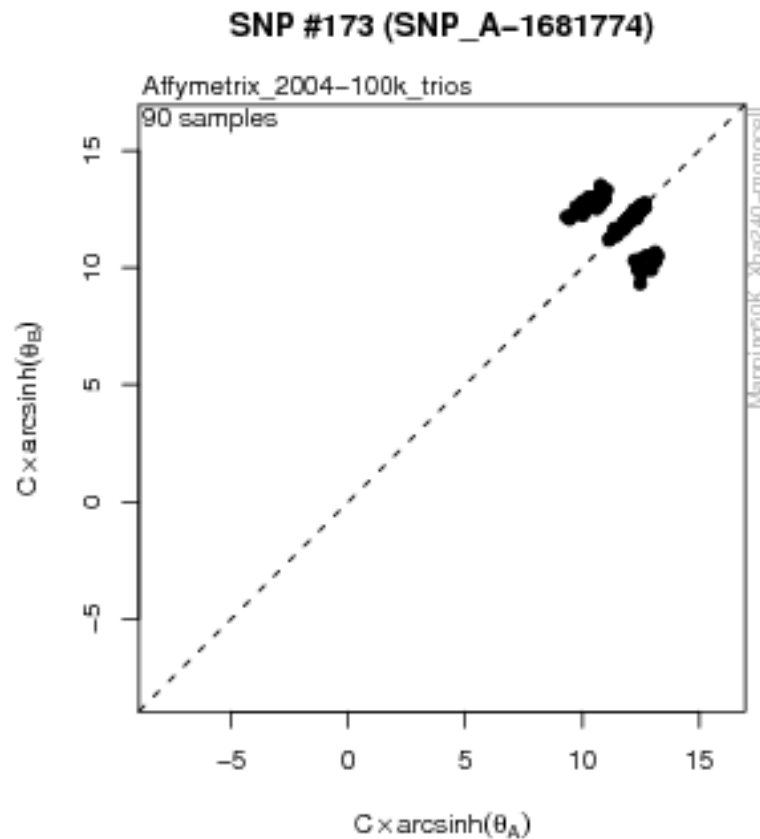


With calibration:

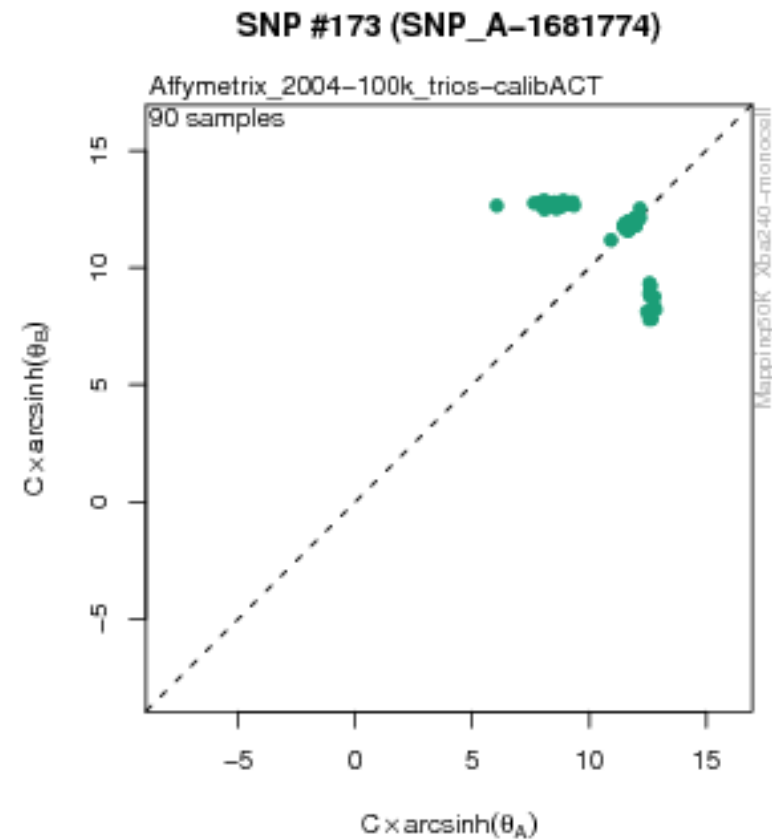


A more subtle example

Without calibration:

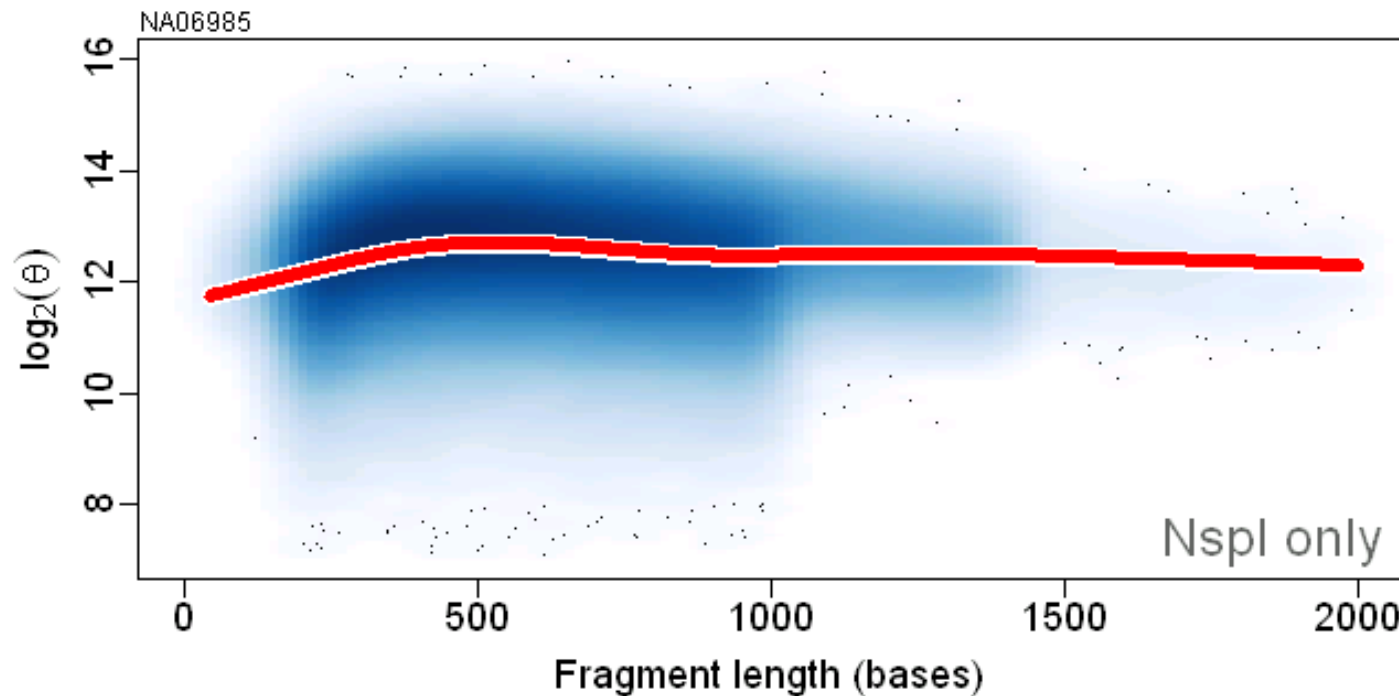


With calibration:



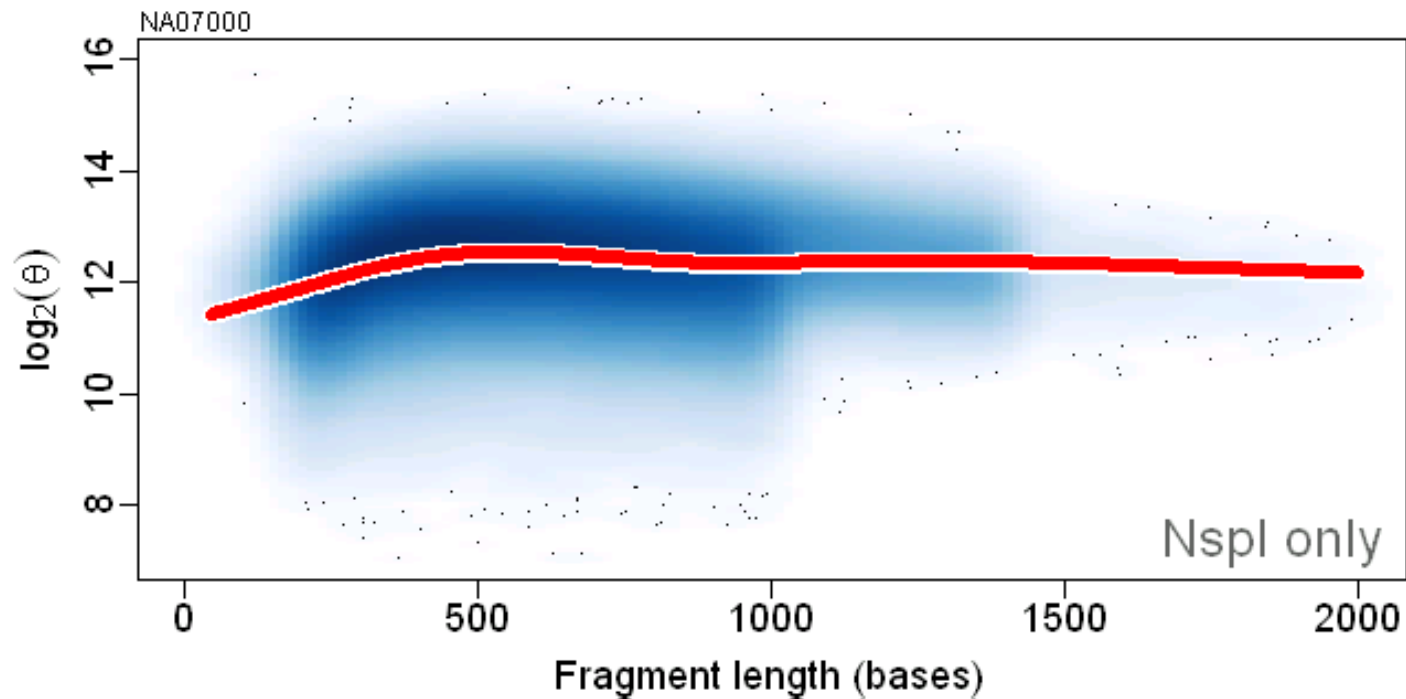
Fragment length normalization

Longer fragments are amplified less by PCR
Observed as weaker θ signals



Note, here we study the effect on non-polymorphic signals, that is, for SNPs we first do $\theta_{ij} = \theta_{ijA} + \theta_{ijB}$.

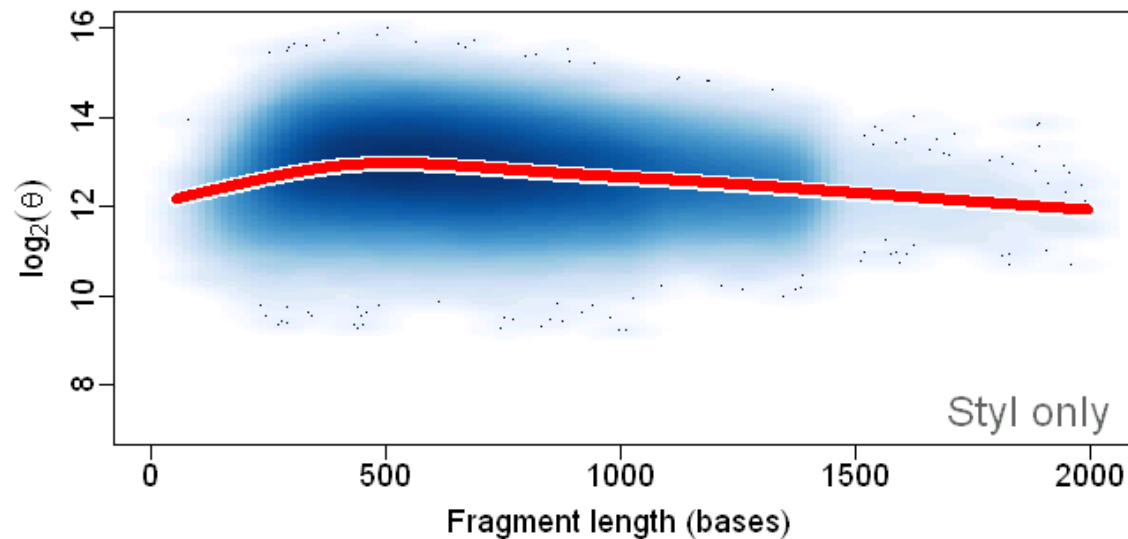
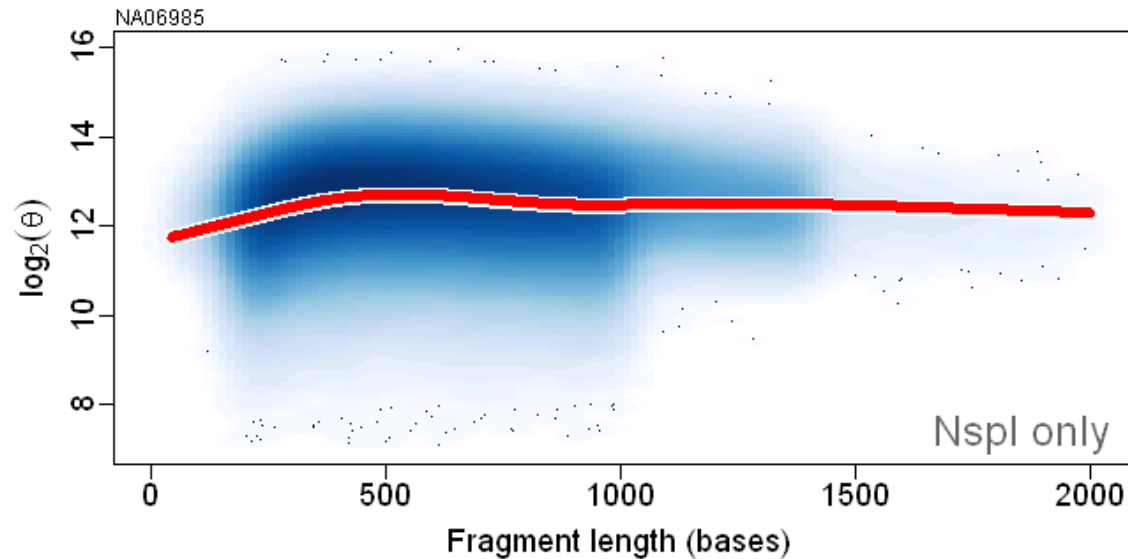
Slightly different effects between arrays
adds extra variation



Fragment-length normalization for multi-enzyme hybridizations

- For **GWS5 and GWS6**, the DNA is fragmented using **two enzymes**.
- For all CN probes, all targets originate from *Nspl* digestion.
- For SNP probes, some targets originate exclusively from *Nspl*, exclusively from *Styl*, or from **both *Nspl* and *Styl***.

Fragment-length effects for co-hybridized enzymes are assumed to be additive



Fragment-length normalization for co-hybridized enzymes

Multi-enzyme normalization model:

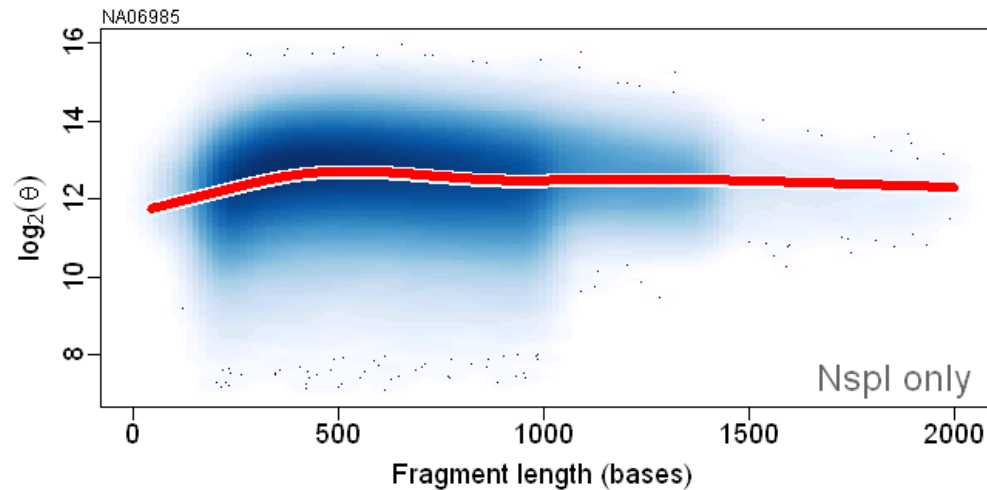
$$\log_2 \theta_j^* \leftarrow \log_2 \theta_j - \delta^*$$

$$\delta^* = \delta(\lambda_{\text{Nsp},j}, \lambda_{\text{Sty},j}) = \text{correction}$$

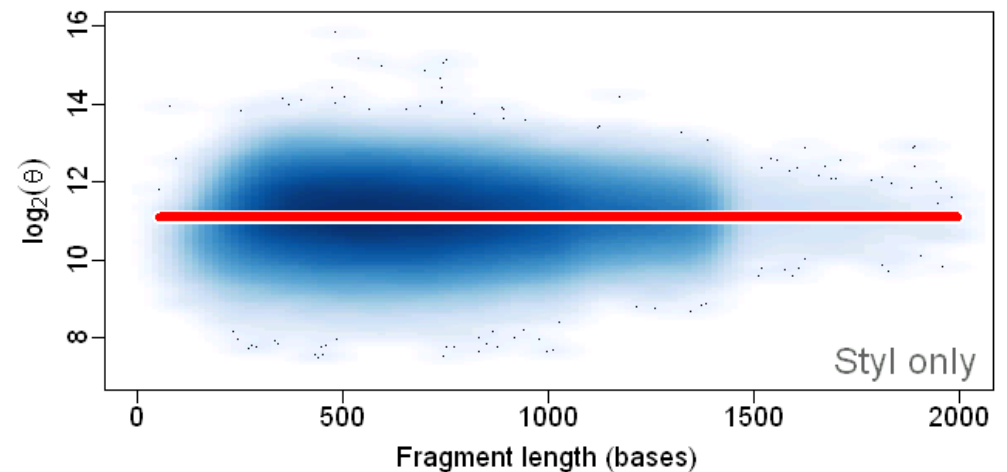
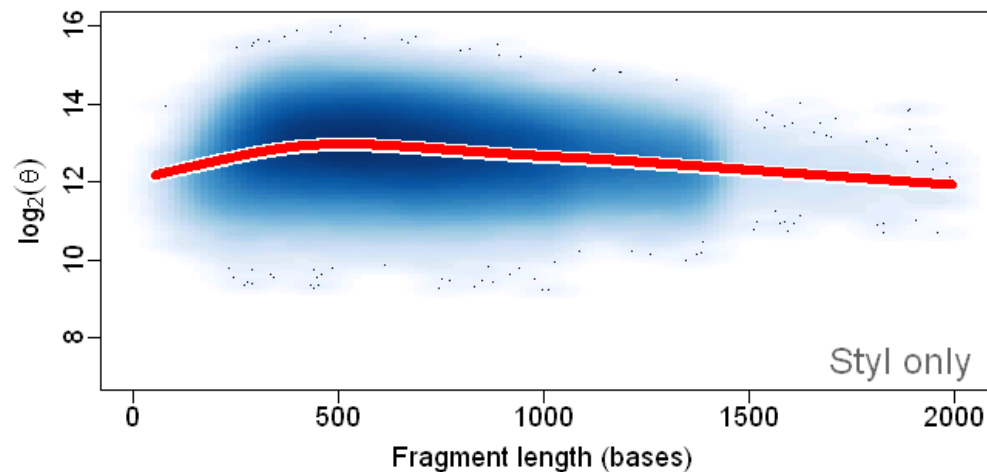
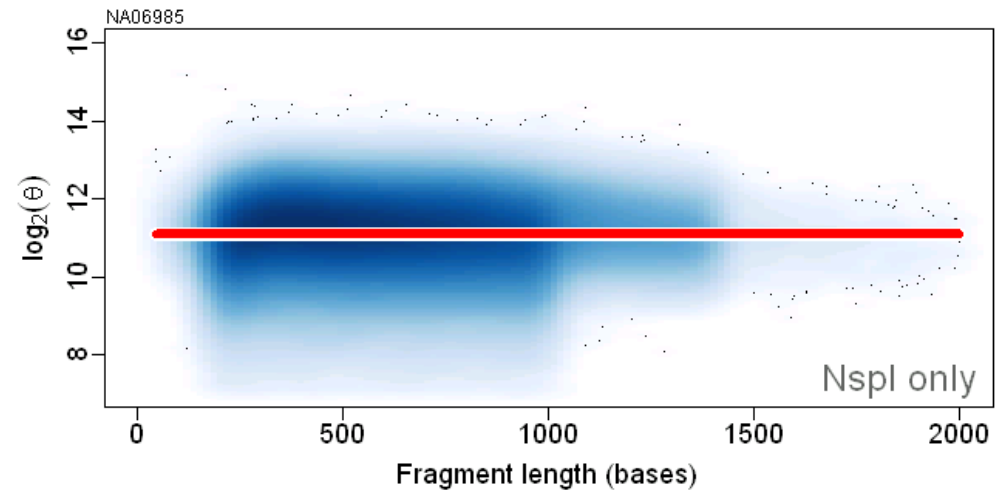
$\lambda_{\text{Nsp}}, \lambda_{\text{Sty}}$ = fragment lengths in *Nspl* and *Styl*.

Multi-enzyme fragment-length normalization removes the effects

Array #1 before

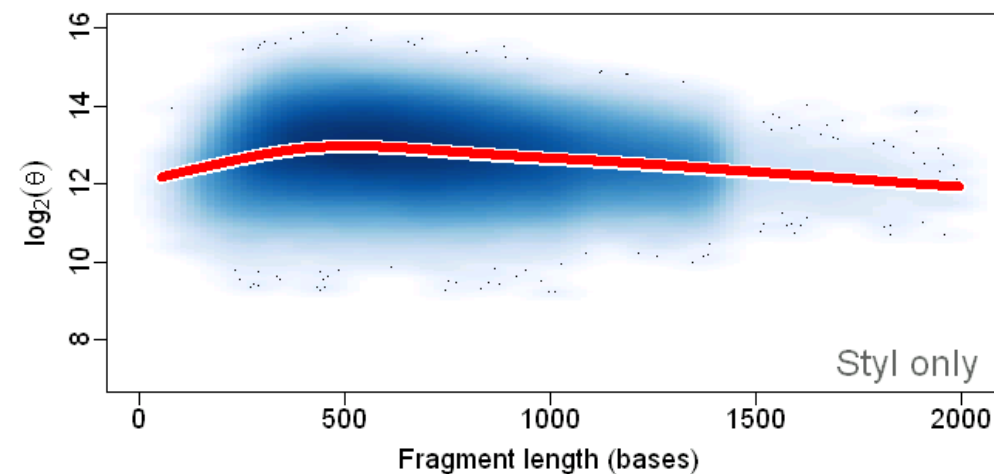
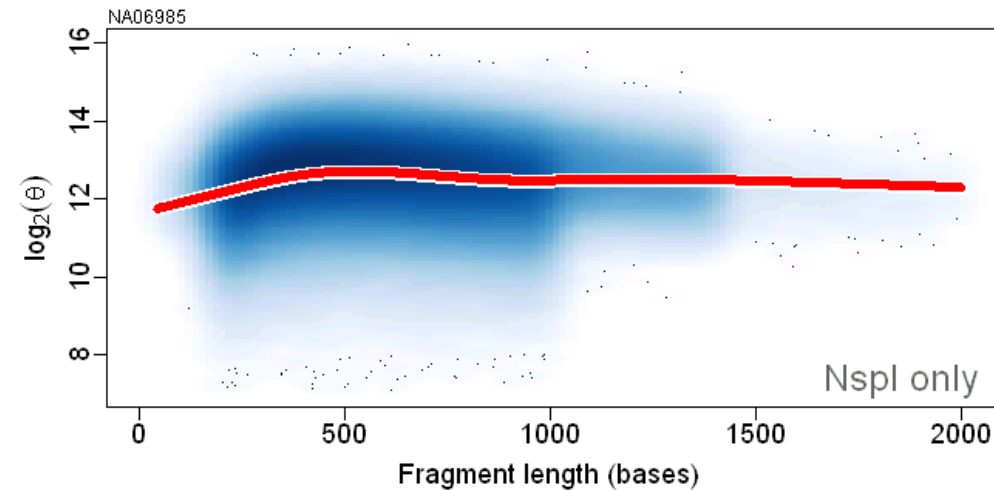


Array #1 after



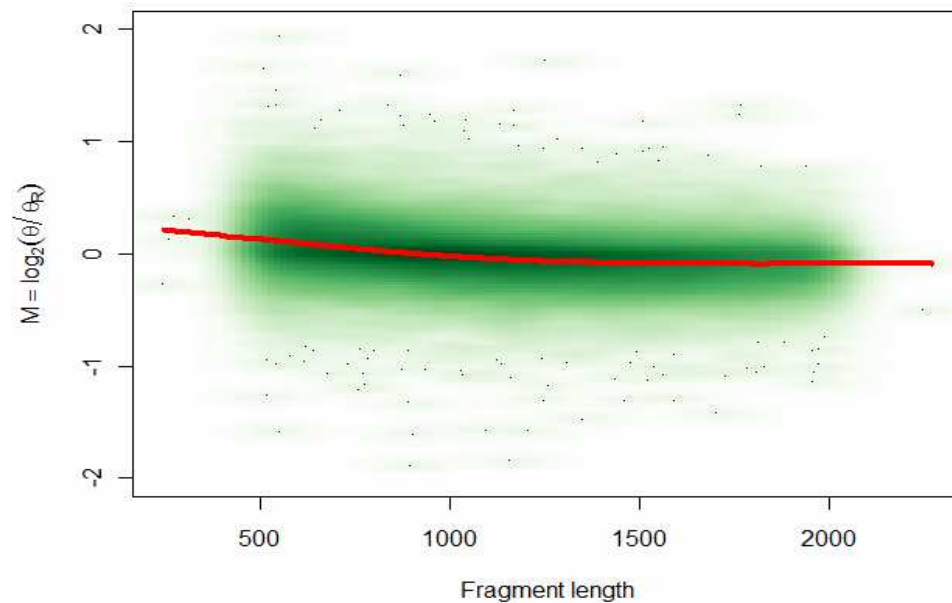
Multi-enzyme fragment-length normalization removes the effects

Array#1 before

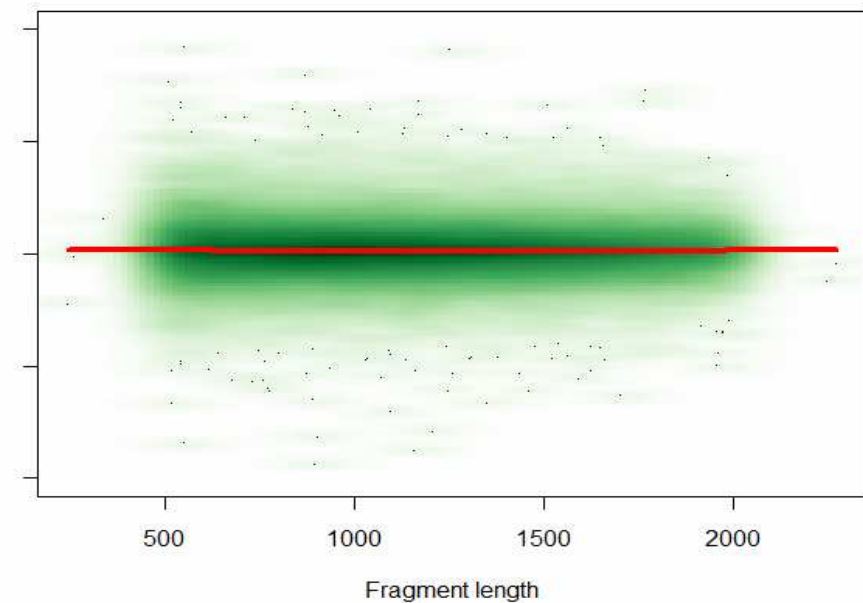


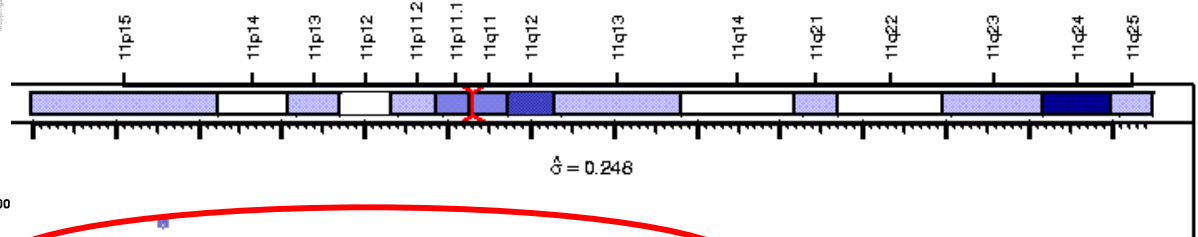
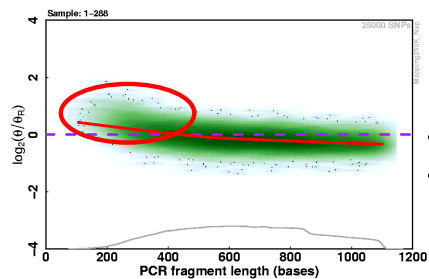
Removing the effect on the chip effects,
will also remove the effect on CN log ratios

Before:

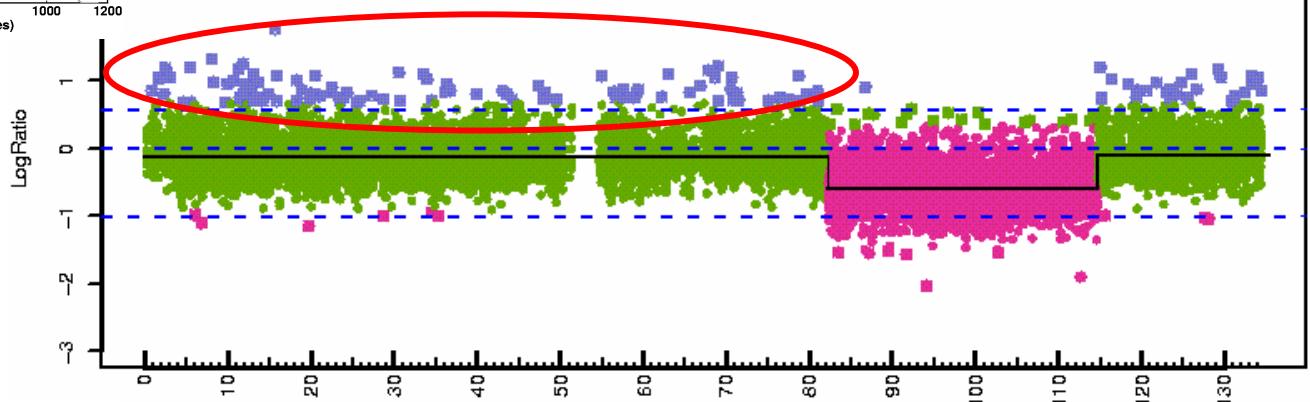


After:

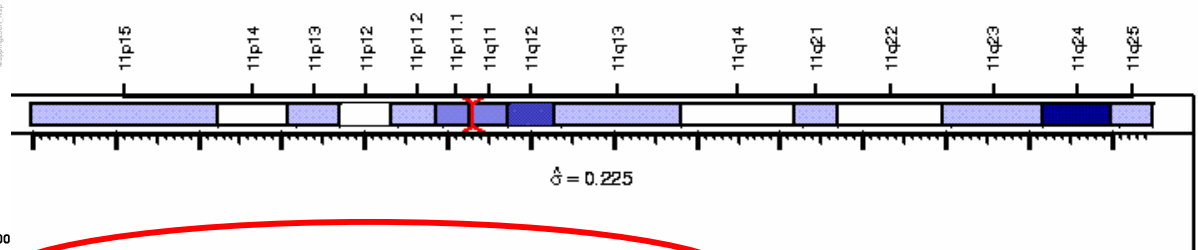
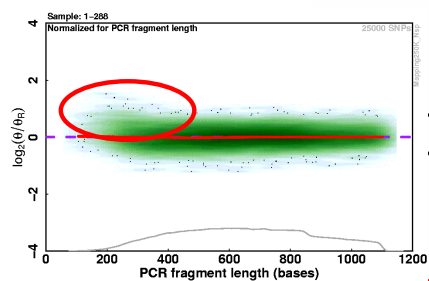




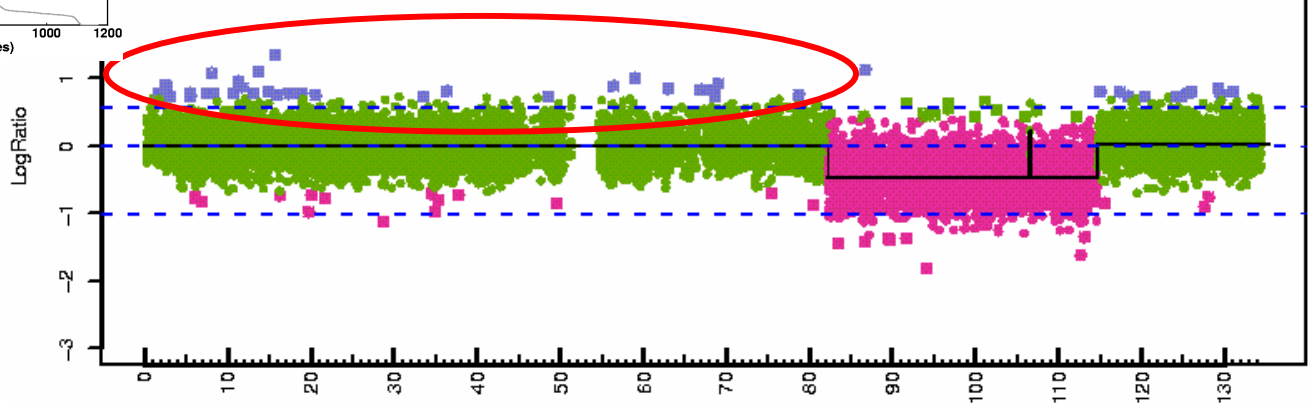
Before



$$\sigma = 0.246$$



After



$$\sigma = 0.225$$

aroma.affymetrix

You will need:

- Affymetrix CDF, e.g. GenomeWideSNP_6.cdf
- A Unit Fragment Length file, e.g. GenomeWideSNP_6.ufl

```
fln <- FragmentLengthNormalization(ces, target="zero")  
cesN <- process(fln)
```


**Finally,
a convenient
transform**

Bijjective transform of $(\theta_{ijA}, \theta_{ijB})$ in to $(\theta_{ij}, \beta_{ij})$.

Transform $(\theta_{ijA}, \theta_{ijB})$ to $(\theta_{ij}, \beta_{ij})$ by:

Non-polymorphic SNP signal: $\theta_{ij} = \theta_{ijA} + \theta_{ijB}$

Allele B frequency signal: $\beta_{ij} = \theta_{ijB} / \theta_{ij}$

A CN probe does not have a β_{ij} . However, both CN probes and SNPs have a non-polymorphic signal θ_{ij} .

We expect the following:

Genotype BB: $\theta_{ijB} \gg \theta_{ijA} \Rightarrow \beta_{ij} \approx 1$

Genotype AA: $\theta_{ijB} \ll \theta_{ijA} \Rightarrow \beta_{ij} \approx 0$

Genotype AB: $\theta_{ijB} \approx \theta_{ijA} \Rightarrow \beta_{ij} \approx 1/2$

Thus, θ_{ij} carry information on CN and β_{ij} on genotype.

Copy numbers are estimated relative to a reference

Relative copy numbers:

$$C_{ij} = 2^{*(\theta_{ij} / \theta_{Rj})}$$

Alternatively, log-ratios:

$$M_{ij} = \log_2(\theta_{ij} / \theta_{Rj})$$

Note: C_{ij} is defined also when $\theta \leq 0$, but M_{ij} is not.

Array $i=1,2,\dots,I$. Locus $j=1,2,\dots,J$.

Allele-specific copy numbers

Allele-specific copy numbers (C_{ijA}, C_{ijB}):

$$C_{ijA} = 2 * (\theta_{ijA} / \theta_{Rj})$$
$$C_{ijB} = 2 * (\theta_{ijB} / \theta_{Rj})$$

Note that,

1. $C_{ij} = C_{ijA} + C_{ijB} = 2 * (\theta_{ijA} + \theta_{ijB}) / \theta_{Rj} = 2 * (\theta_{ij} / \theta_{Rj})$
2. $C_{ijB} / C_{ij} = [2 * (\theta_{ijB} / \theta_{Rj})] / [2 * (\theta_{ij} / \theta_{Rj})] = \theta_{ijB} / \theta_{ij} = \beta_{ij}$
3. $C_{ijB} = 2 * (\theta_{ijB} / \theta_{ij}) * (\theta_{ij} / \theta_{Rj}) = \beta_{ij} * C_{ij}$

aroma.affymetrix

You will need:

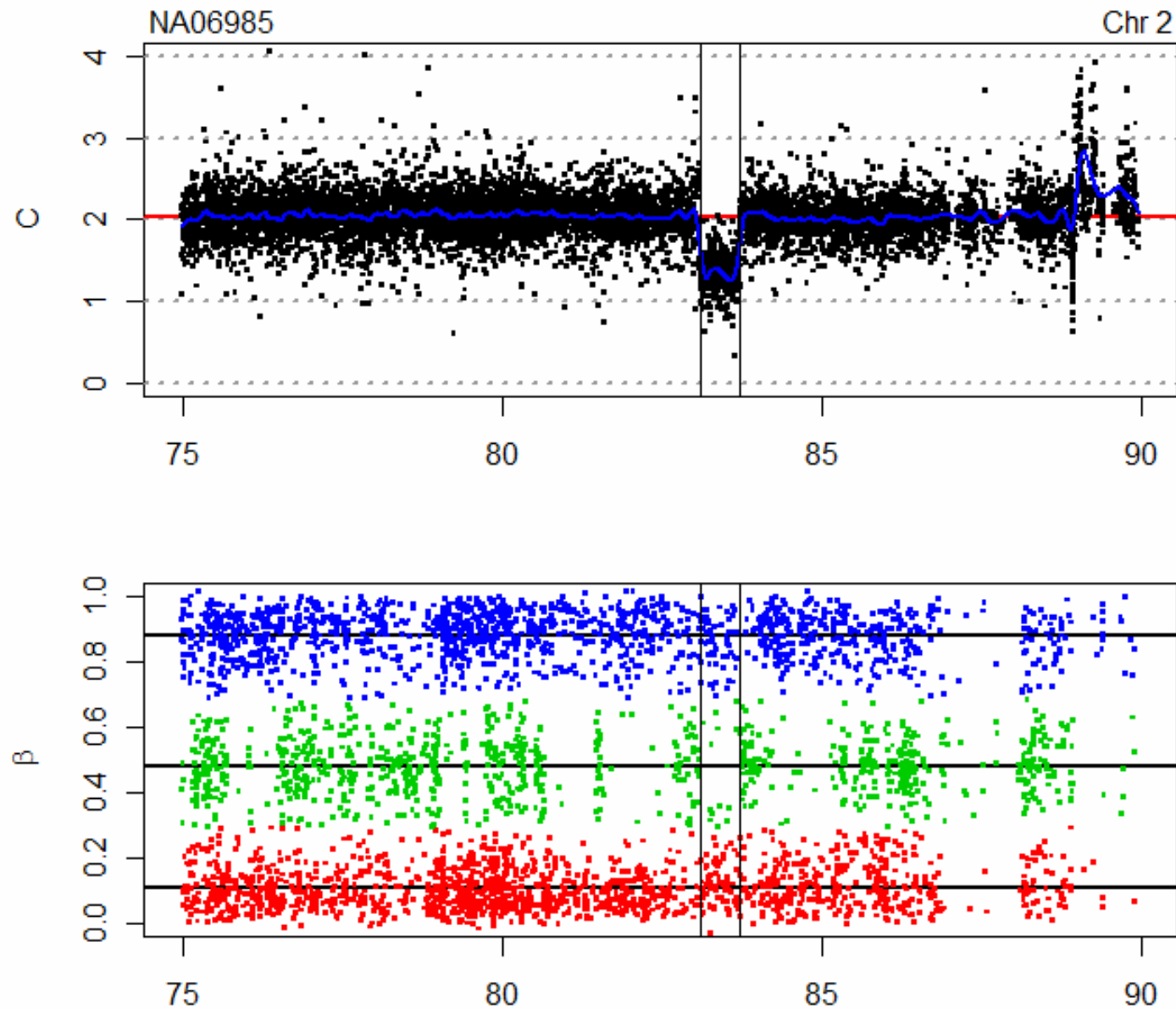
- Affymetrix CDF, e.g. GenomeWideSNP_6.cdf
- A Unit Genome Position file, e.g. GenomeWideSNP_6.ugp

```
data <- extractTotalAndFreqB(cesN)
theta <- data[, "total", ]
freqB <- data[, "freqB", ]
```

Plot Array 3 along chromosome 2

```
gi <- getGenomeInformation(cdf)
units <- getUnitsOnChromosome(gi, 2)
pos <- getPositions(gi, units)
plot(pos, theta[units, 3])
plot(pos, freqB[units, 3])
```

CN and freqB - (C, β) - along genome



Selecting reference samples

The choice of reference sample(s) is important
- *A real example from my postdoc projects*

Data set:

- 3 Affymetrix 250K Nsp arrays.
- Processed at the AGRF / WEHI, Melbourne, Australia.

Reference sets:

- Public: 270 normal HapMap arrays (“gold standard”).
- In-house: 11 anonymous/unknown(!) AGRF arrays.

segmentation regions found with reference

set:

(i) 11 in-house samples and (i) 270 HapMap
samples

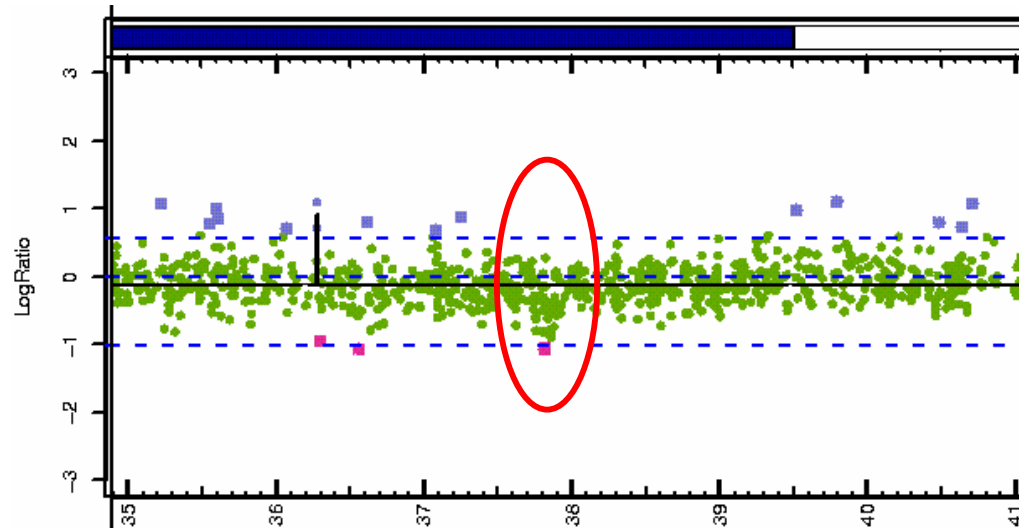
sample	chr	length	#SNPs	log2CN		AGRF	HapMap
A	9	1,023	3	0.50	gain	X	
A	20	5,161	3	-0.47	loss	X	
A	13	10,770	3	0.50	gain	X	
A	10	26,774	3	-0.25	loss	X	
A	5	34,423	3	-0.44	loss	X	
B	4	47,982	3	0.65	gain	X	
B	14	22,269	5	0.45	gain	X	X
A	6	37,028	6	-0.34	loss	X	
C	6	37,028	6	-0.32	loss	X	
C	3	38,218	7	-0.39	loss	X	
A	3	39,082	8	-0.43	loss	X	
A	11	21,357	11	-0.30	loss	X	
A	10	90,838	12	0.29	gain	X	
A	14	153,137	25	0.41	gain	X	X
B	14	153,137	25	0.76	gain	X	X
C	14	153,137	25	0.55	gain	X	X
B	22	225,133	31	0.37	gain	X	
B	13	297,921	36	-0.30	loss	X	
B	8	171,547	37	-0.34	loss	X	
A	14	411,453	70	-0.21	loss	X	
A	23	2,696,994	169	0.34	loss	X	
C	23	2,696,994	169	0.40	gain	X	poorly
B	11	32,485,465	3823	-0.39	loss	X	X
A	21	37,006,554	3936	0.17	trisomy	X	
Count						25	6
Fraction						100%	24%

Stronger signal with in-house reference set

Example: A 37 SNP deletion on chr 8

HapMap

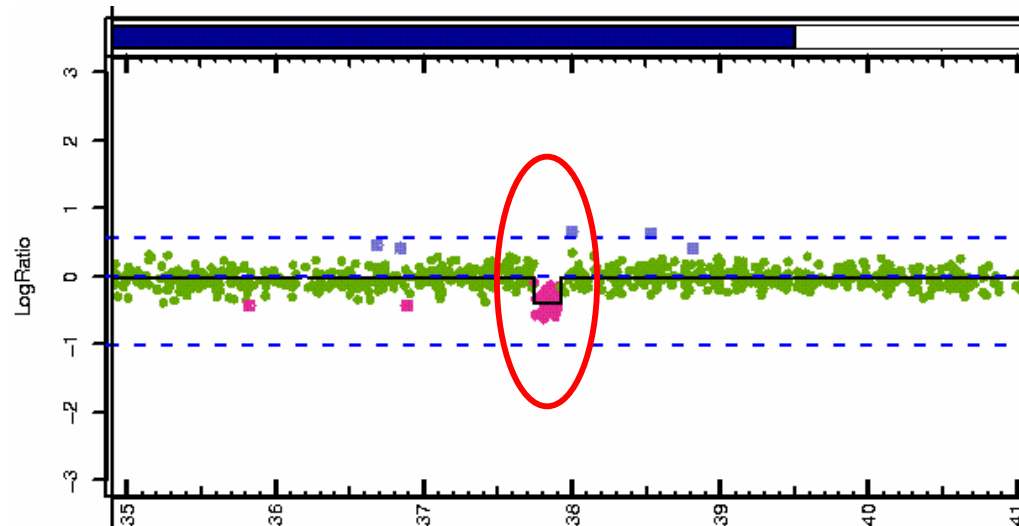
270 samples



$$\sigma = 0.237$$

AGRF

11 anonymous
samples



$$\sigma = 0.126$$

Conclusion

It is better to use a small,
even unknown, reference set
from the same microarray lab
than an external reference set.

Summary of CRMA v2

	CRMA v2
Preprocessing (probe signals)	1. Allelic crosstalk calibration 2. Probe-sequence normalization
Summarization	Robust averaging: CN probes: $\theta_{ij} = PM_{ij}$ SNPs: $\theta_{ijA} = \text{median}_k(PM_{ijkA})$ $\theta_{ijB} = \text{median}_k(PM_{ijkB})$ array i , loci j , probe k .
Post-processing	PCR fragment-length normalization
Transform	$(\theta_{ijA}, \theta_{ijB}) \Rightarrow (\theta_{ij}, \beta_{ij})$ $\theta_{ij} = \theta_{ijA} + \theta_{ijB}$, $\beta_{ij} = \theta_{ijB} / \theta_{ij}$
Allele-specific & total CNs	$C_{ijA} = 2^{*(\theta_{ijA} / \theta_{Rj})}$ and $C_{ijB} = 2^{*(\theta_{ijB} / \theta_{Rj})}$ $C_{ij} = 2^{*(\theta_{ij} / \theta_{Rj})}$ reference R

Single array method

CRMA v2 is a single-array preprocessing method

- CRMA v2 estimates chip effects of one array independently of other arrays.
 - It does not use prior parameter estimates etc.
 - A reference signals is only needed when calculating relative CNs, i.e. $C_i = 2^{*(\theta_i/\theta_R)}$.
- Implications:
 - Tumor/normal studies can be done with only two hybridizations.
 - No need to rerun analysis when new arrays are added.
 - Large data sets can be processed on multiple machines.

Evaluation

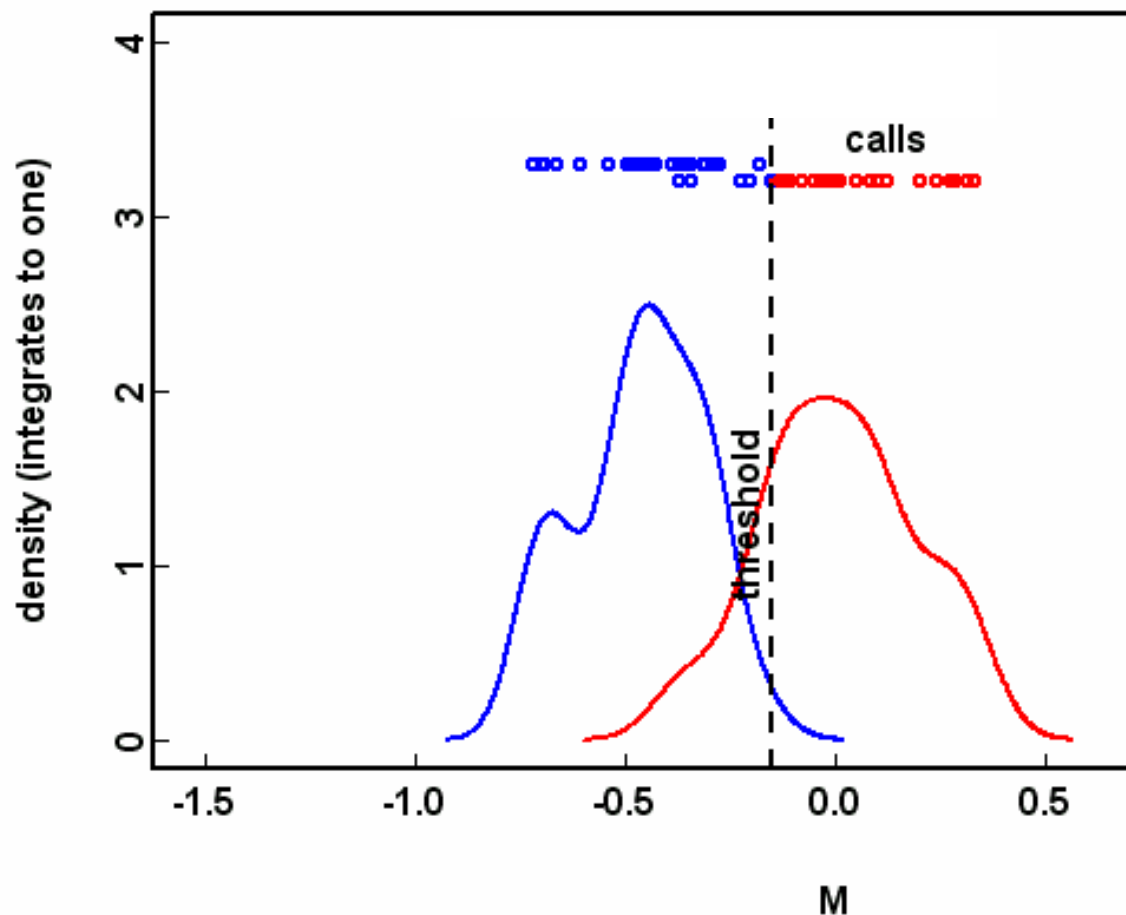
Other methods

	single-array	multi-array	multi-array
	CRMA v2	dChip (Li & Wong 2001)	CN5 (Affymetrix 2006)
Preprocessing (probe signals)	allelic crosstalk. probe-seq norm.	invariant-set	quantile
Summarization (SNP signals θ) and total CNs	i) Robust avg. ii) $\theta = \theta_A + \theta_B$	i) $PM = PM_A + PM_B$ ii) multiplicative	i) log-additive ii) $\theta = \theta_A + \theta_B$
Post-processing	fragment-length. (GC-content)	-	fragment-length. GC-content. Enzyme seq normalization. Genome “wave” normalization
Raw total CNs	$M_{ij} = \log_2(\theta_{ij}/\theta_{Rj})$ [$C_{ij} = 2^*(\theta_{ij}/\theta_{Rj})$]	$M_{ij} = \log_2(\theta_{ij}/\theta_{Rj})$	$M_{ij} = \log_2(\theta_{ij}/\theta_{Rj})$

How well can detect CN changes compare with other methods?

- Other methods:
 - Affymetrix ("CN5") estimates (software GTC v3).
 - dChip estimates (software dChip 2008).
- Data set:
 - 59 GWS6 HapMap samples (29 females & 30 males).
- Evaluation:
 - How well can we detect:
 - CN=1 among CN=2 (ChrX), and
 - CN=0 among CN=1 (ChrY)?
 - At full resolution and various amounts of smoothing.

Calling samples for SNP_A-1920774



males: 30

females: 29

Call rule:

If $M_i < \text{threshold}$, a **male**

Calling a male male:

#True-positives: 30

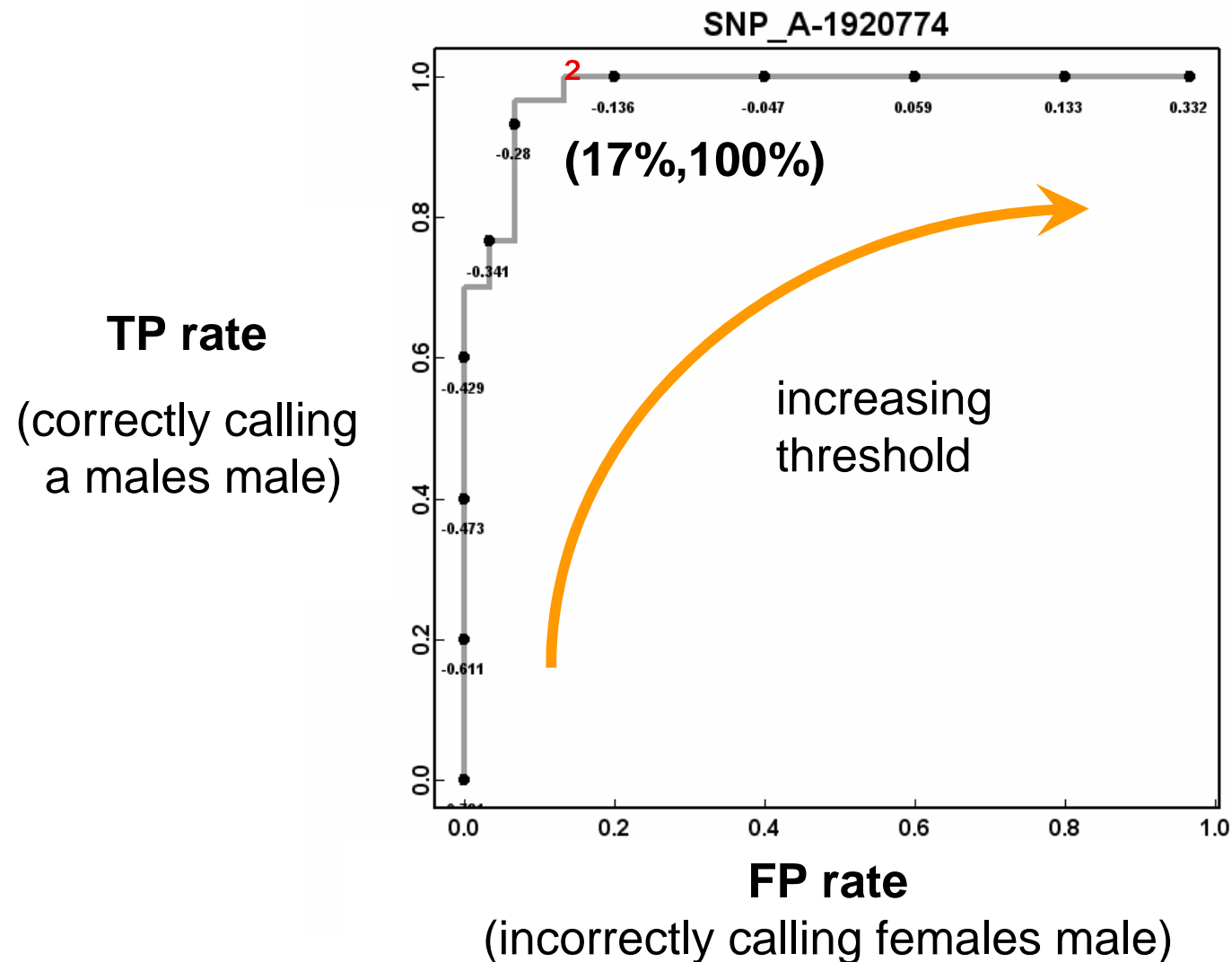
TP rate: 30/30 = 100%

Calling a female male:

#False-positive : 5

FP rate: 5/29 = 17%

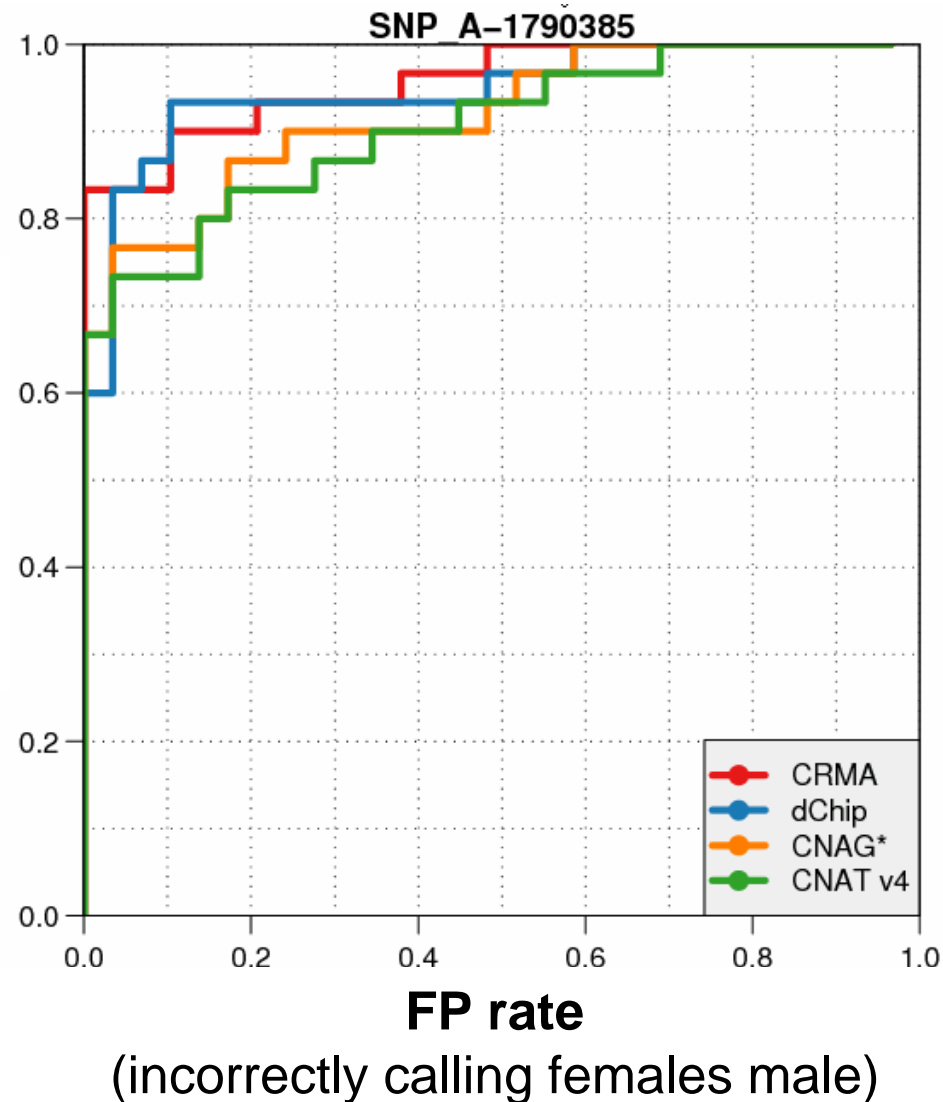
Receiver Operator Characteristic (ROC)



Single-SNP comparison

A random SNP

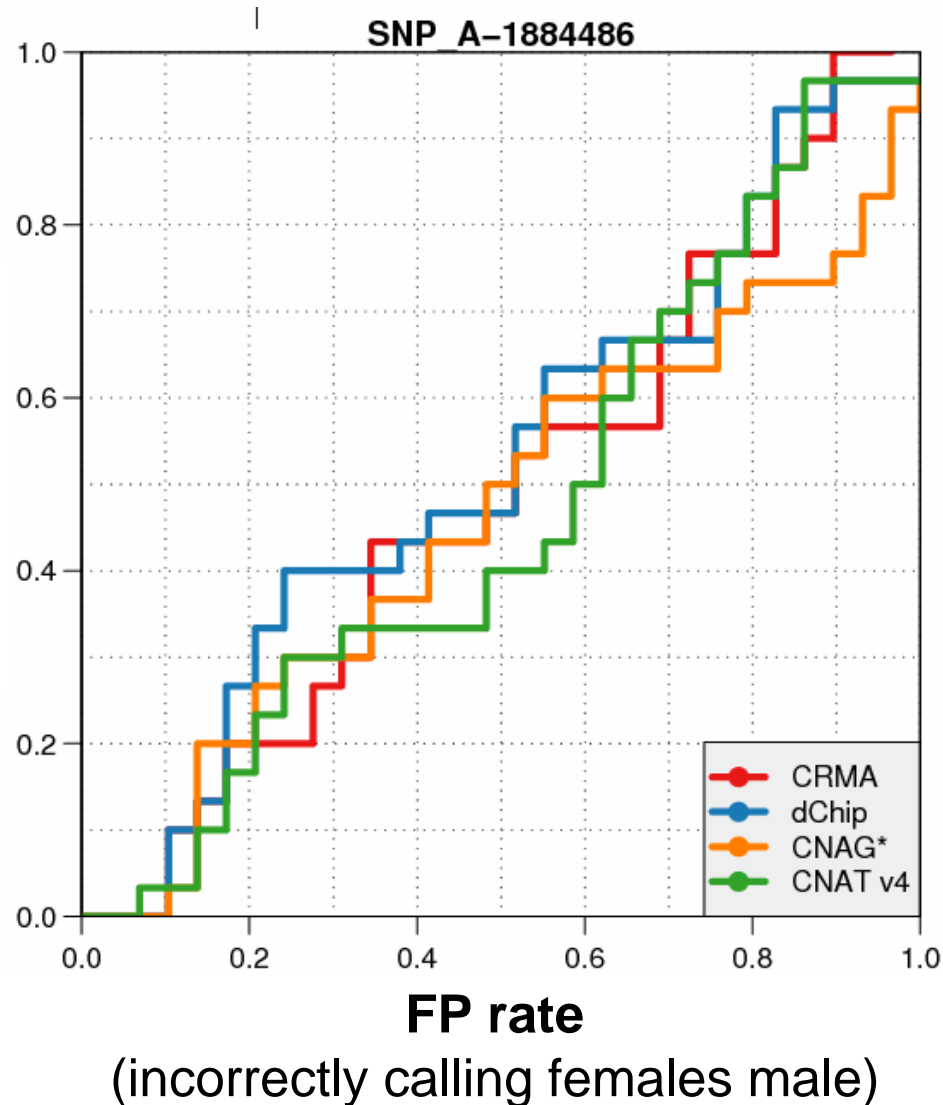
TP rate
(correctly calling
a males male)



Single-SNP comparison

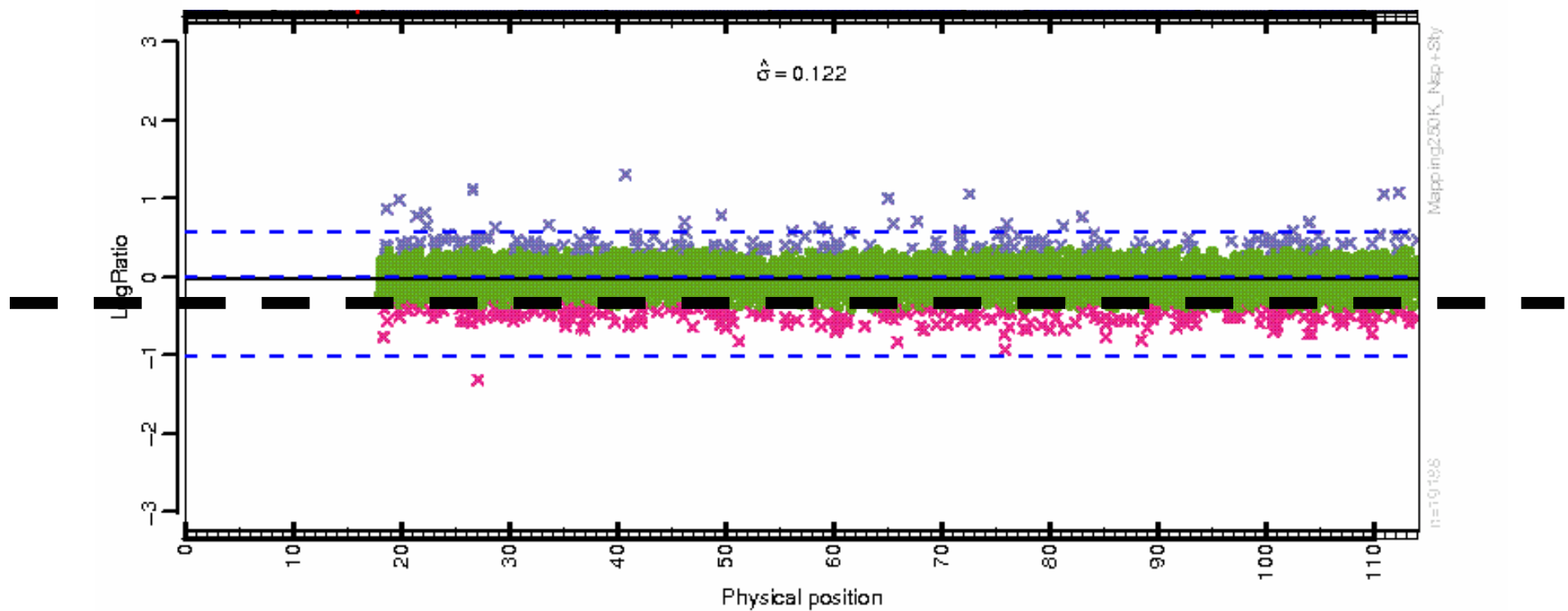
A non-differentiating SNP

TP rate
(correctly calling
a males male)

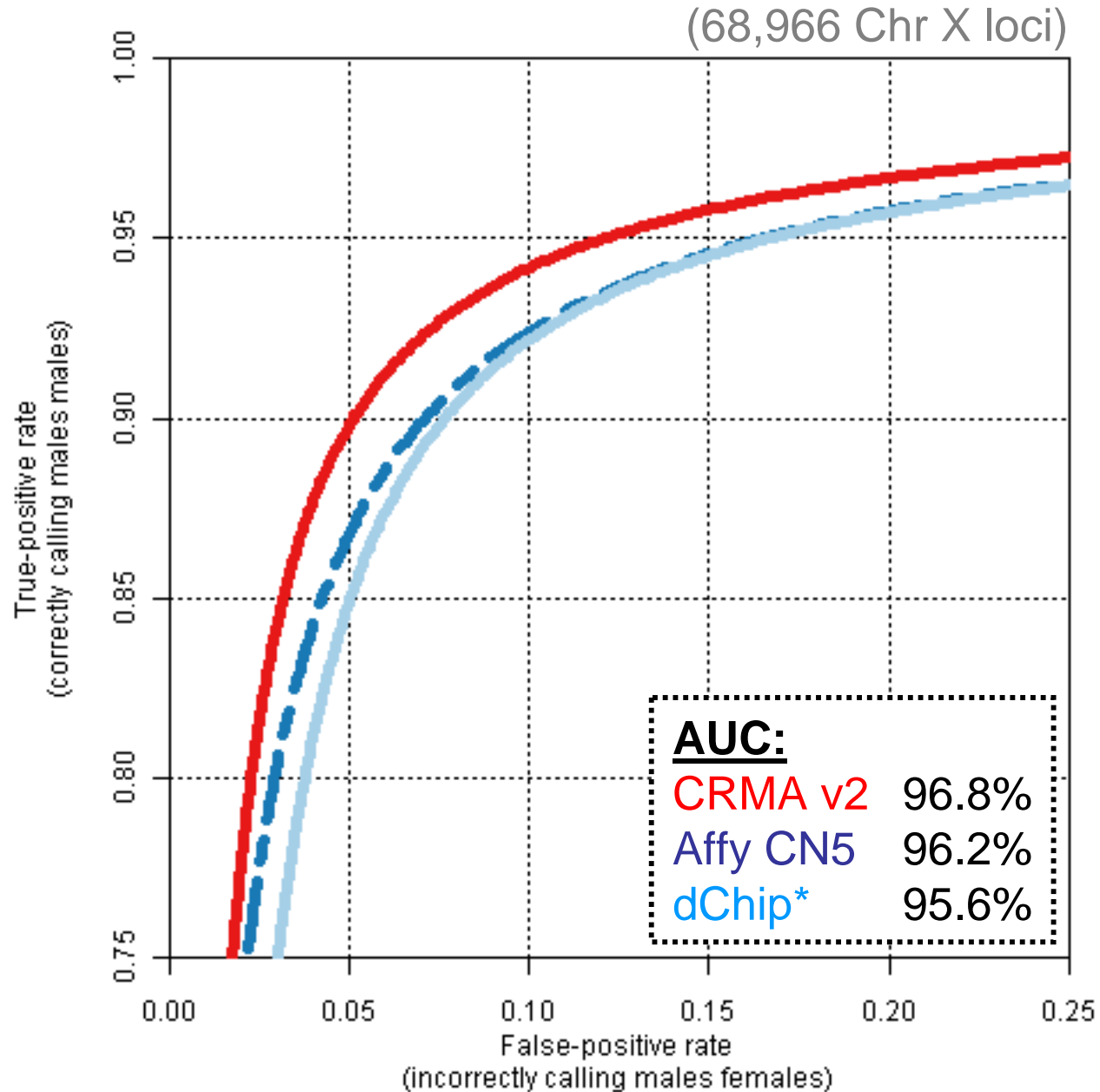


Performance of an average SNP with a common threshold

59 individuals



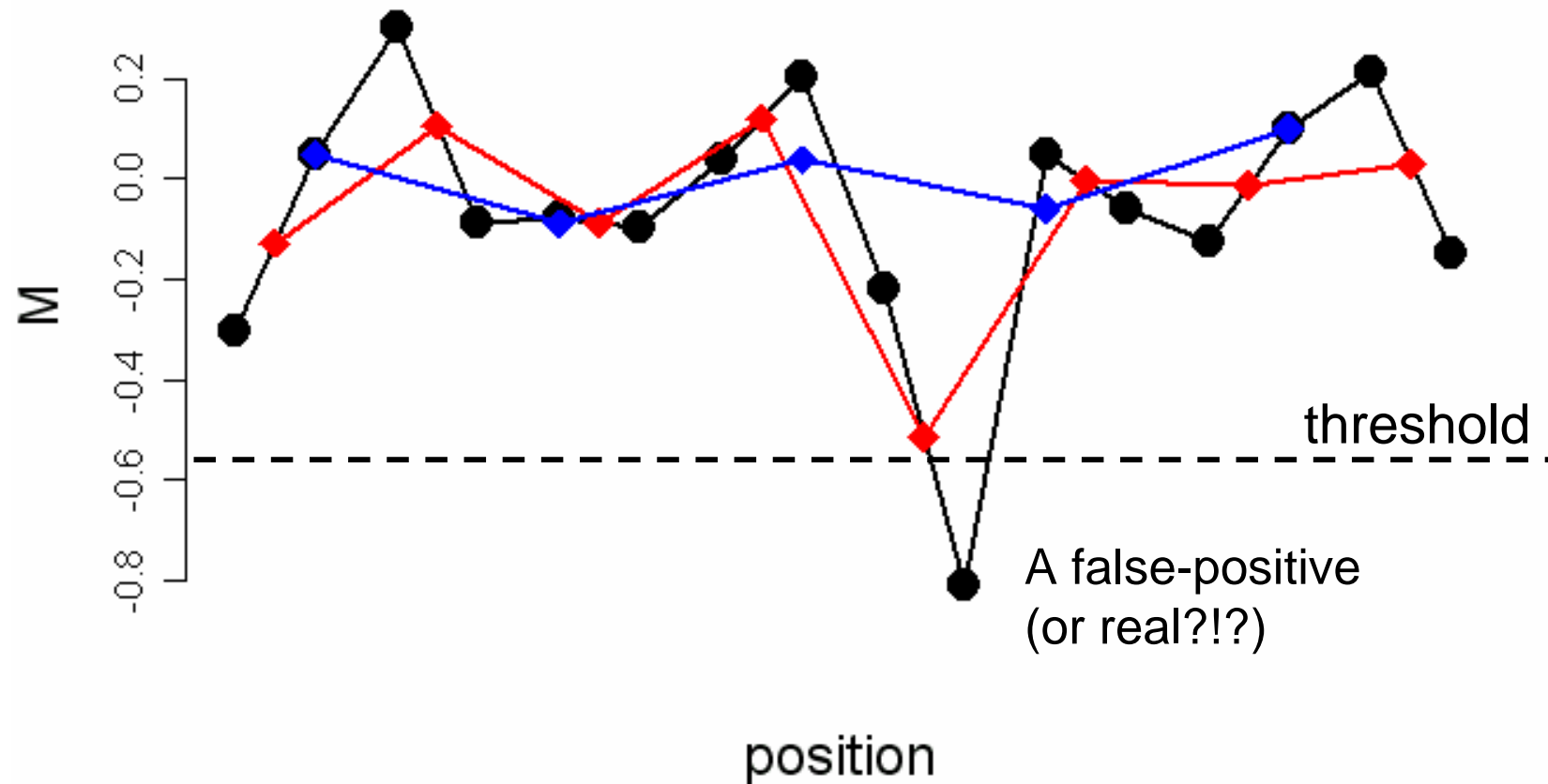
Better detection of CN=1 among CN=2 using CRMA v2



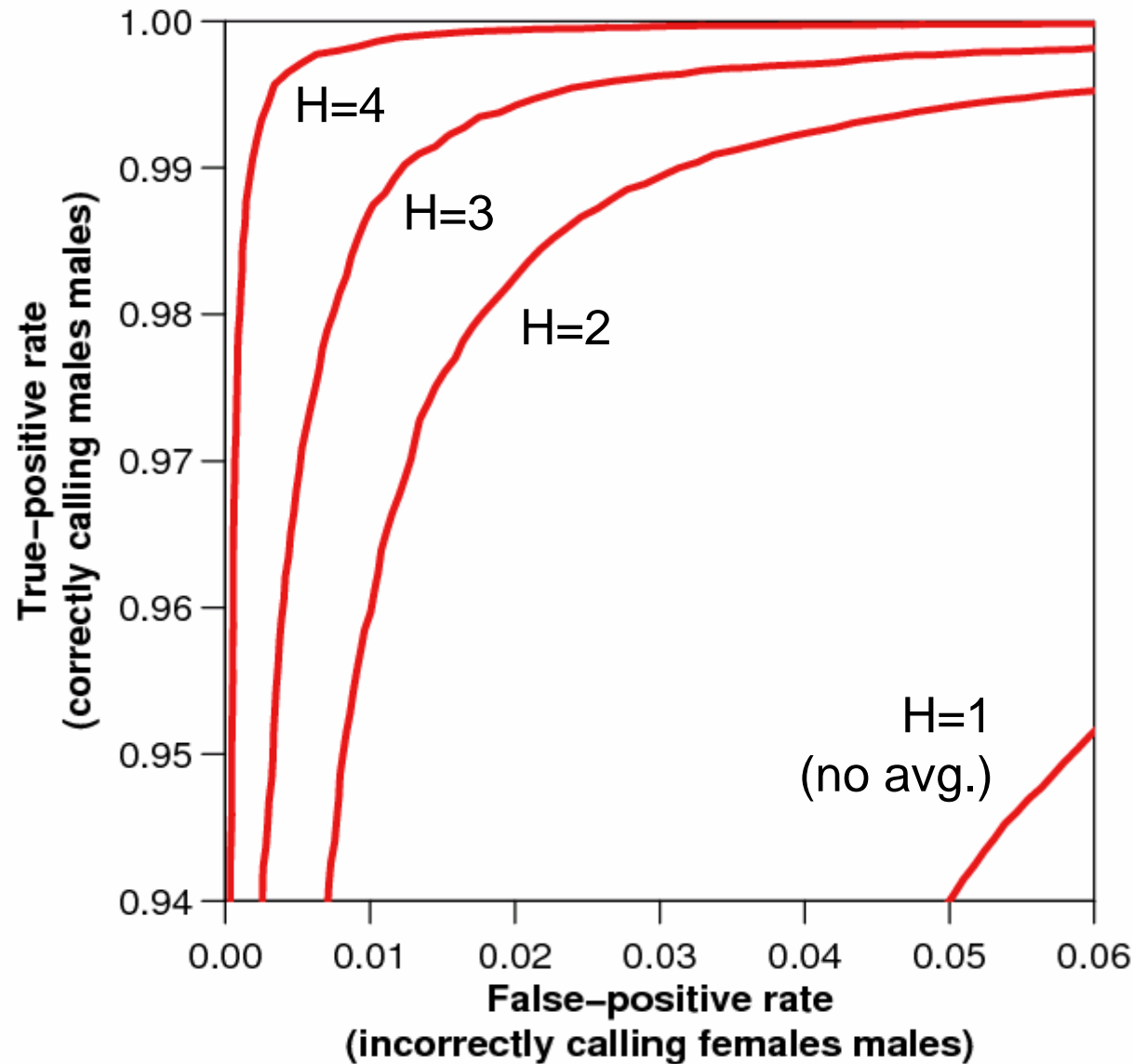
Comparing at
different resolutions

Average across SNPs *non-overlapping windows*

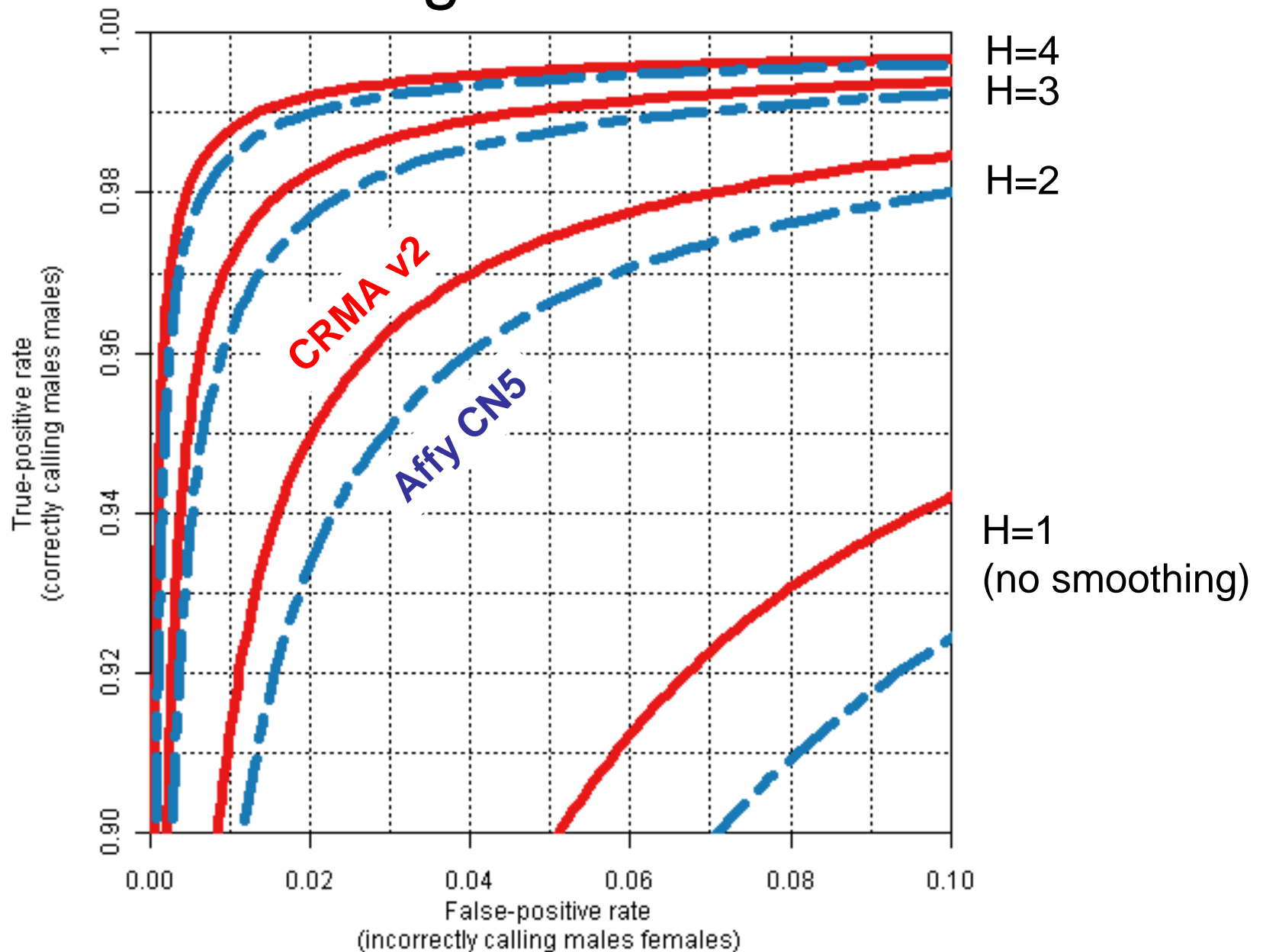
Averaging three and three ($H=3$)



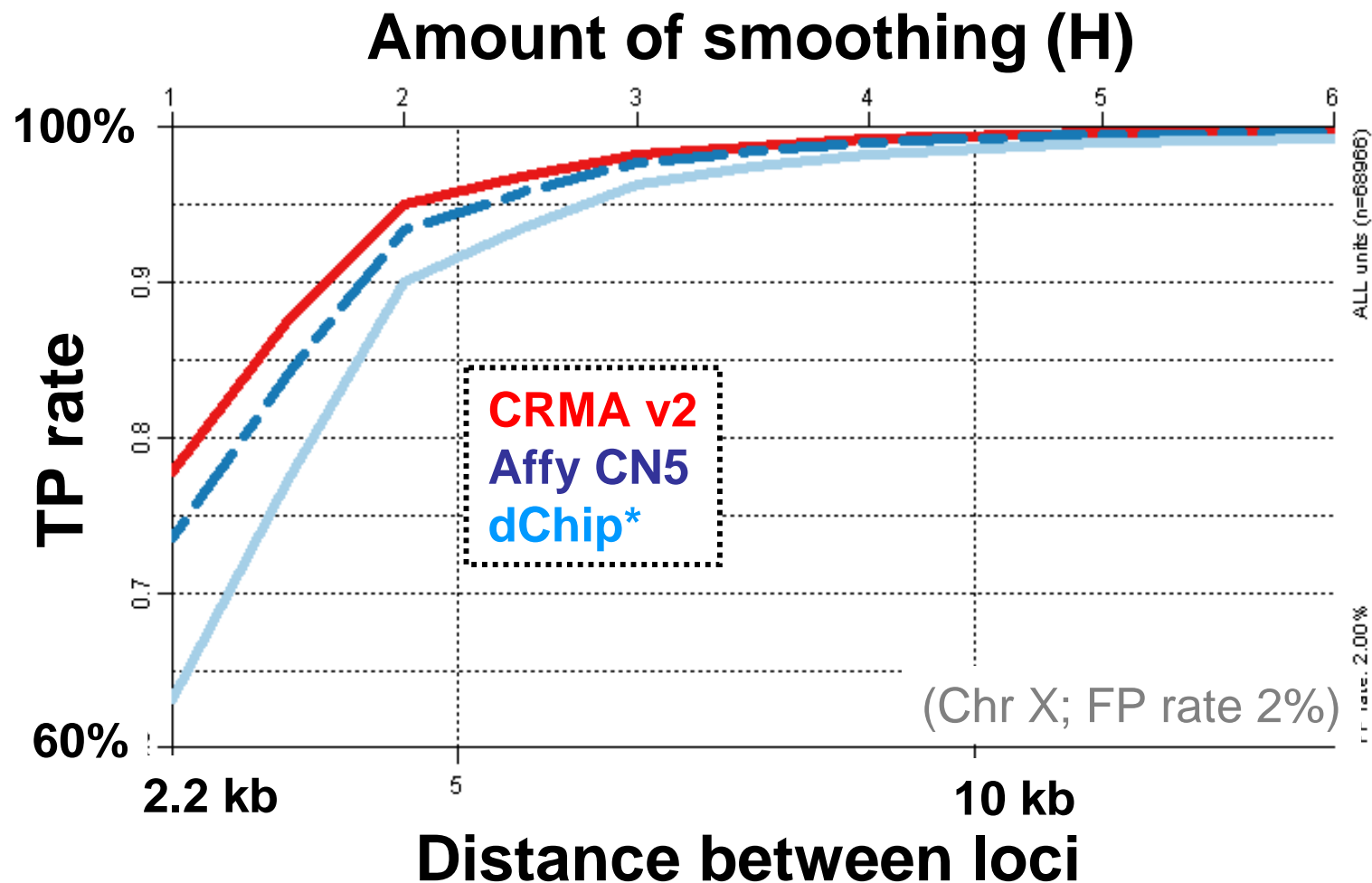
Better detection rate when averaging
(with risk of missing short regions)



CRMA v2 does better
also when smoothing



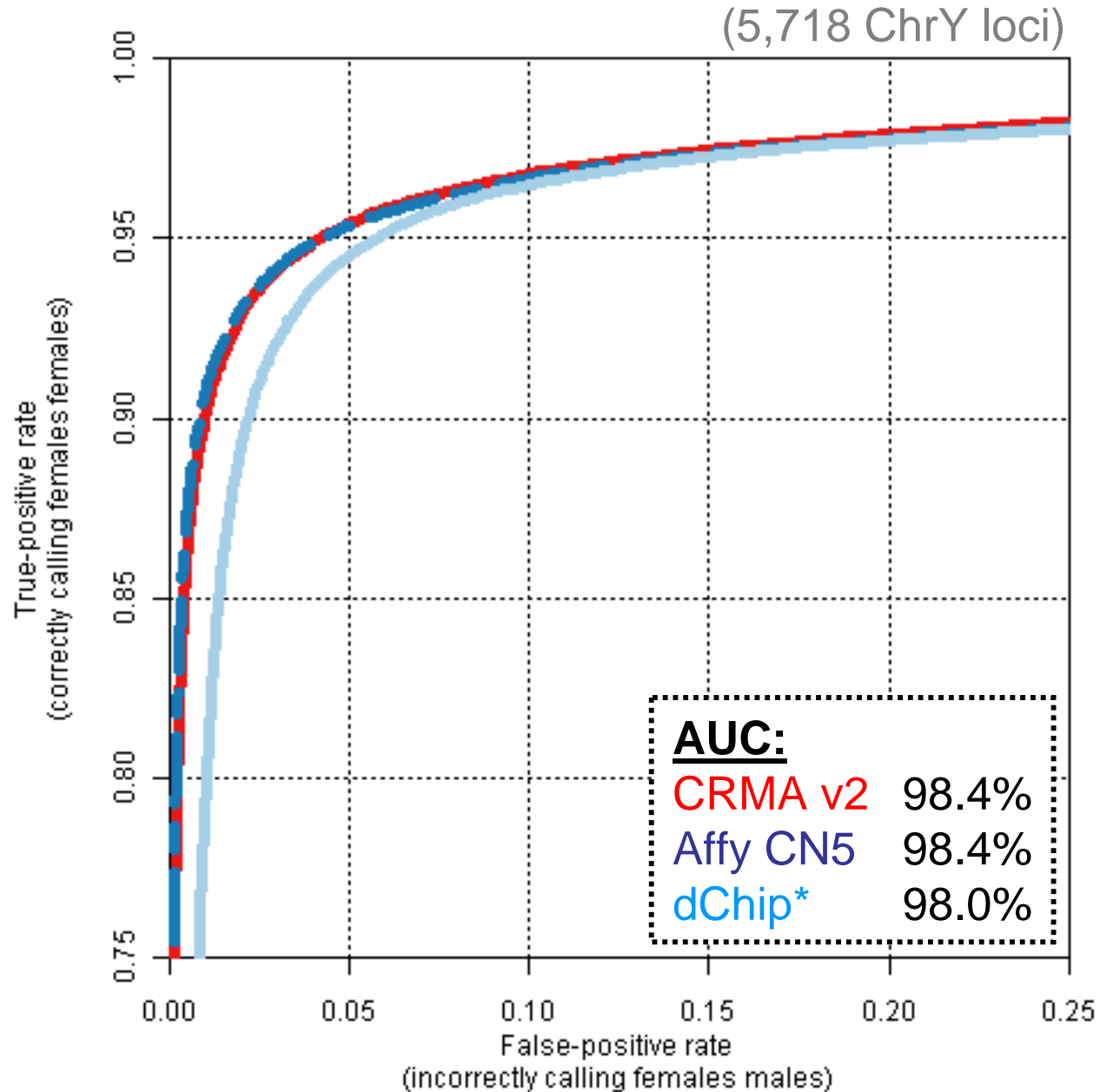
CRMA v2 detects CN=1 among CN=2 better than other at all resolutions



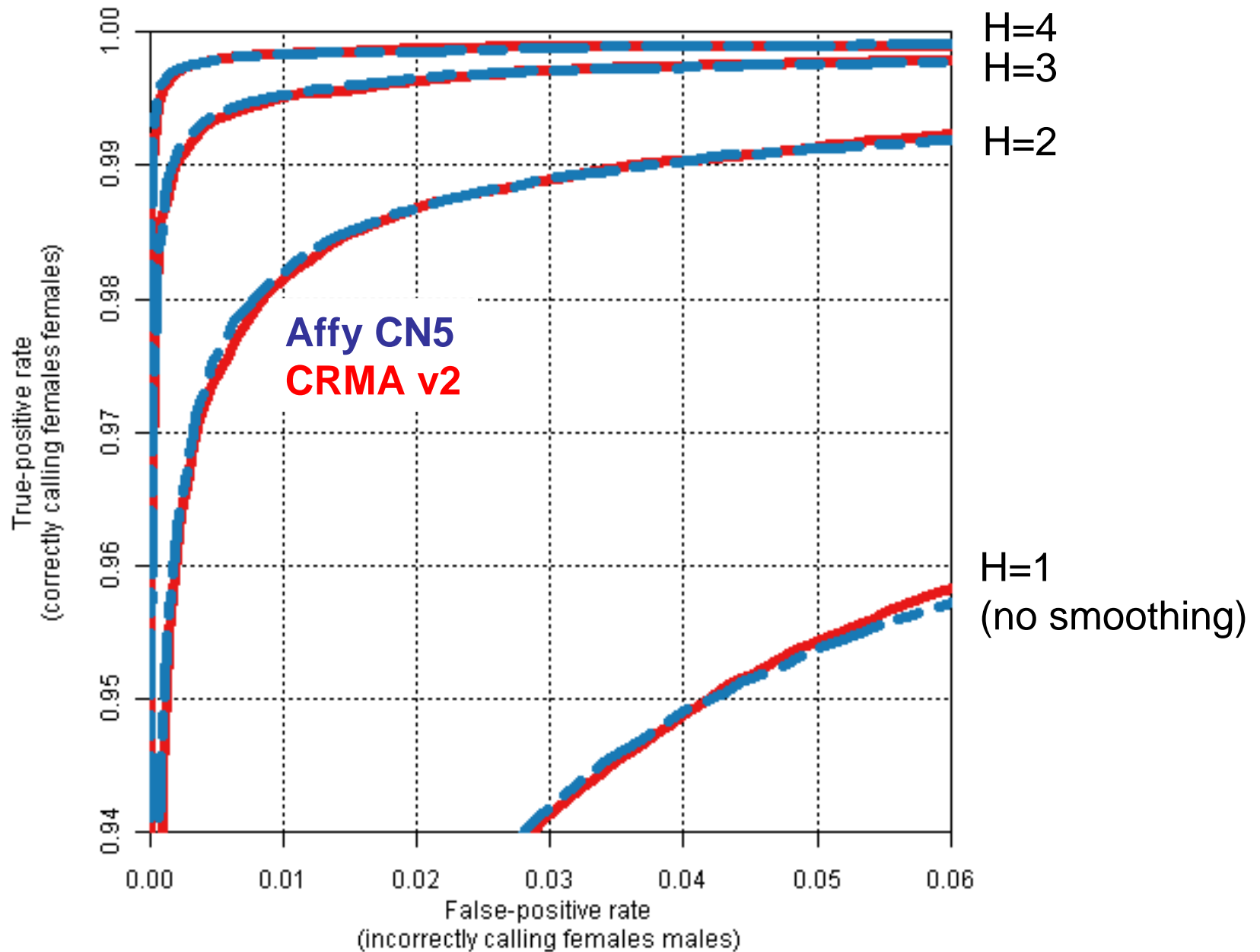
Performance on ChrY

It is easier to detect
CN=0 among CN=1 (ChrY), than
CN=1 among CN=2 (ChrX).

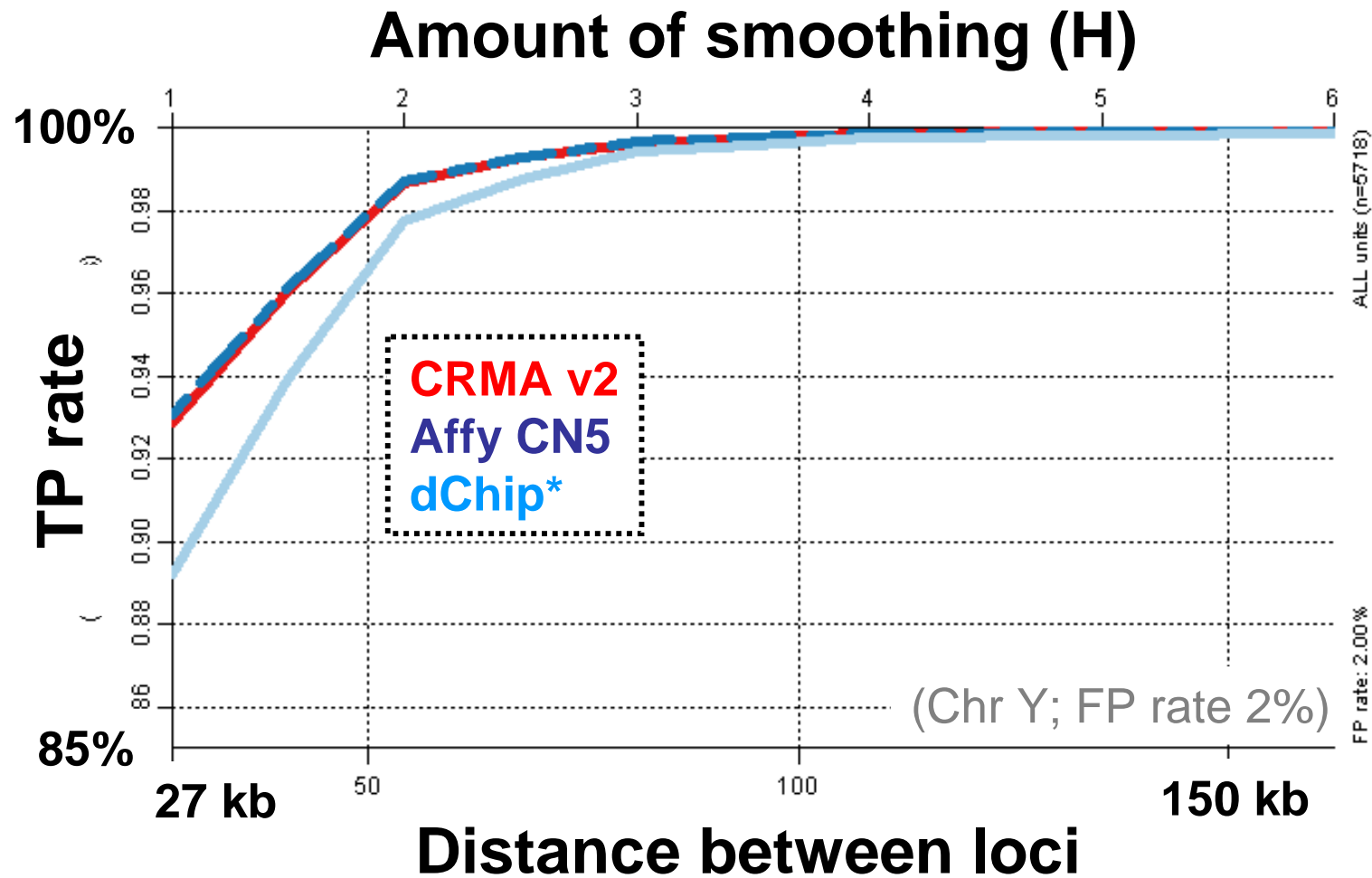
Better detection of CN=0 among CN=1 using CRMA v2/CN5



Similar also when smoothing

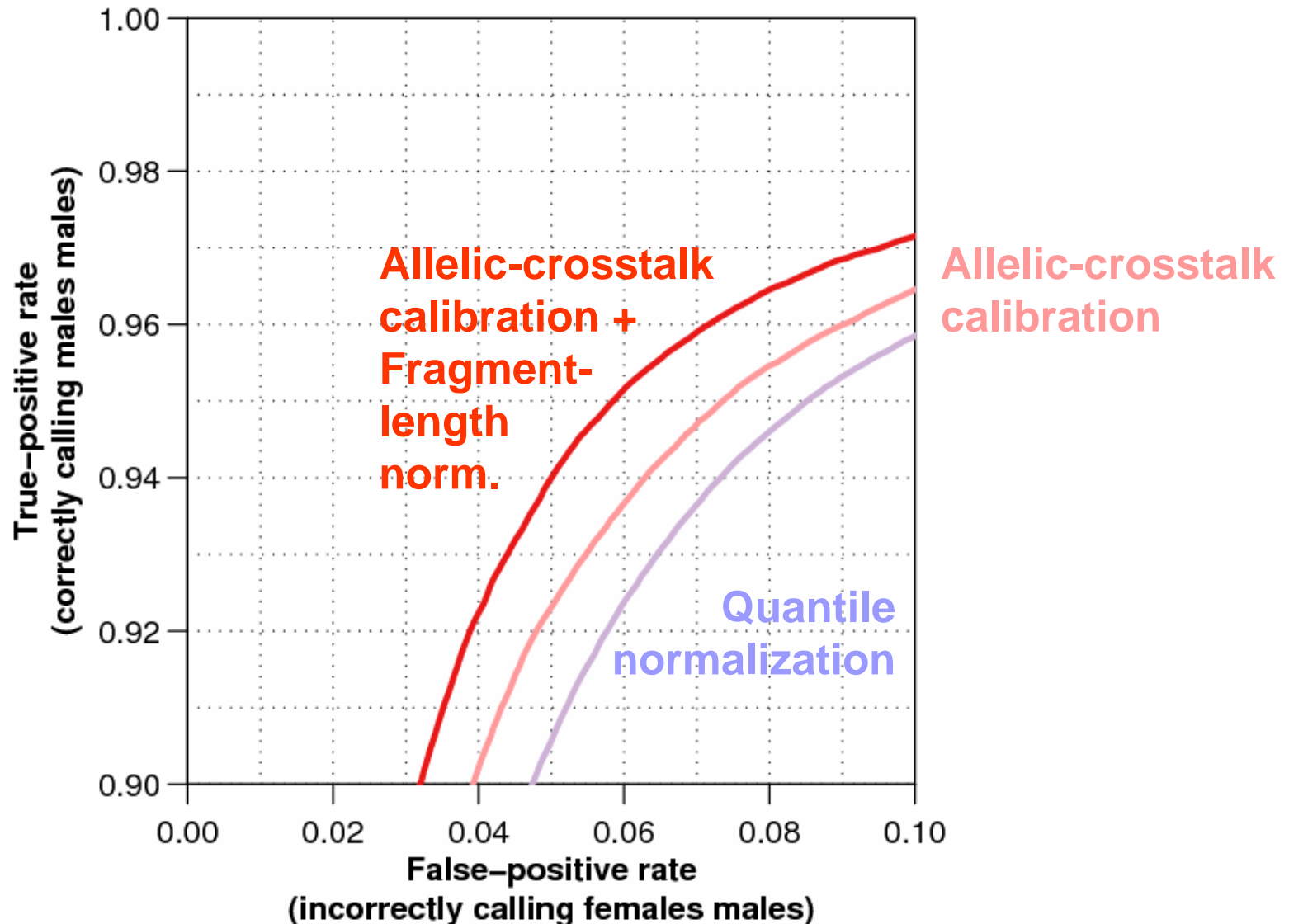


CRMA v2 & CN5 detects CN=0 among CN=1 equally well at different resolutions

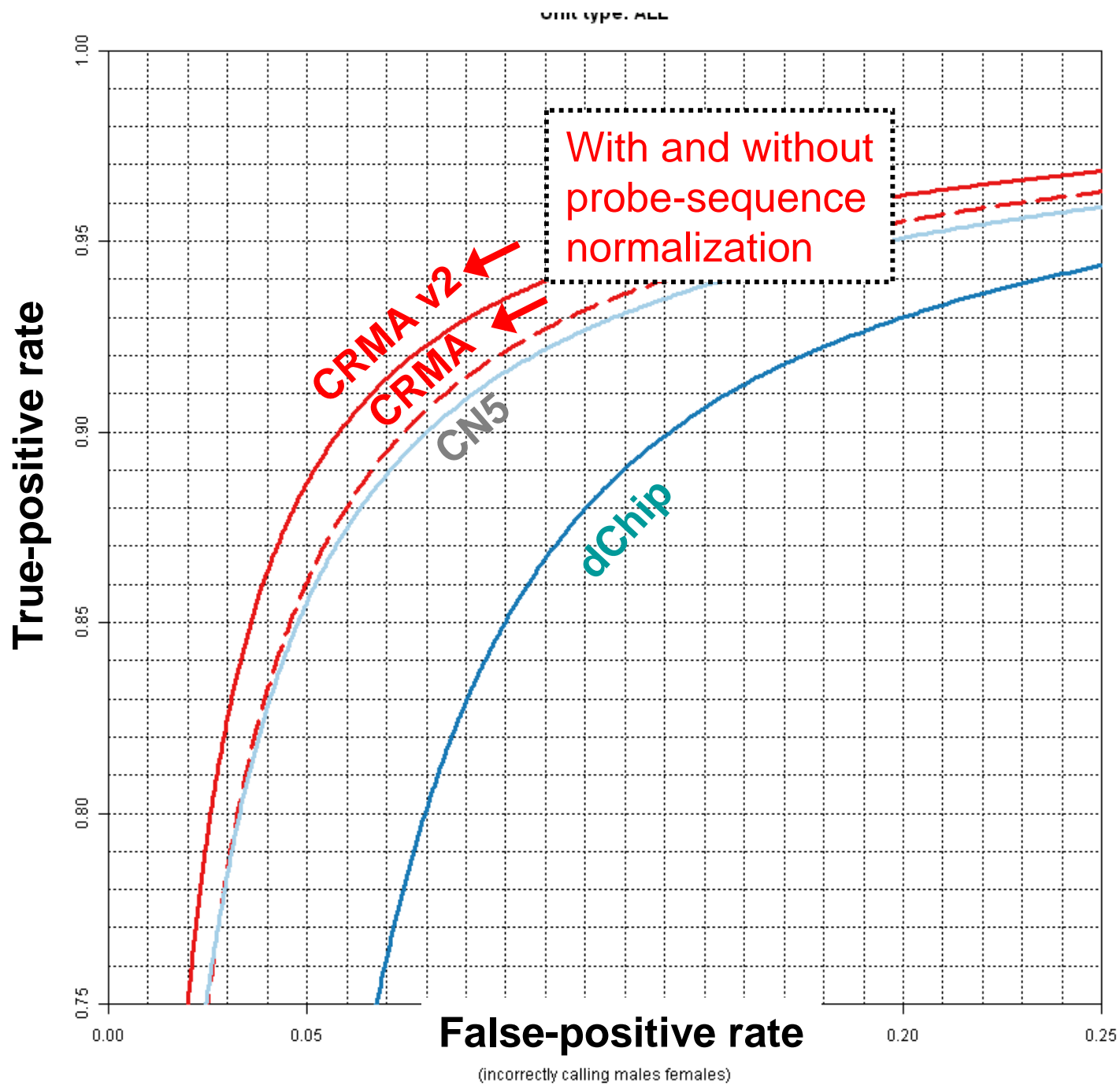


A final revisit of the pre-processing steps

Allelic-crosstalk calibration and PCR fragment length normalization improves the detection rate



Nucleotide-position normalization really helps



Conclusions

Pre-processing helps

- Allelic crosstalk calibration corrects for offset and provides better separation between genotype groups.
- Nucleotide-position normalization corrects for variation across arrays but also heterozygote imbalances.
- PCR fragment-length normalization remove additional variation.
- Using a in-house reference is better than an external one.

Reason for using CRMA v2

- CRMA v2 can differentiate CN=1 from CN=2 better than other methods.
- CRMA v2 & Affymetrix CN5 differentiate CN=0 from CN=1 equally well.
- CRMA v2 applies to all Affymetrix chip types.
- CRMA v2 is a single-array estimator.
- CRMA v2 can be applied immediately after scanning the array.
- There might be a CRMA v3 later ;)

Appendix